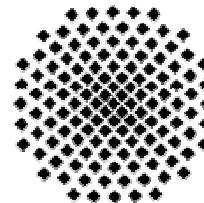


Kioloa, February 8, 2006

Chromium Bose-Einstein Condensates

Luis Santos

Universität Stuttgart



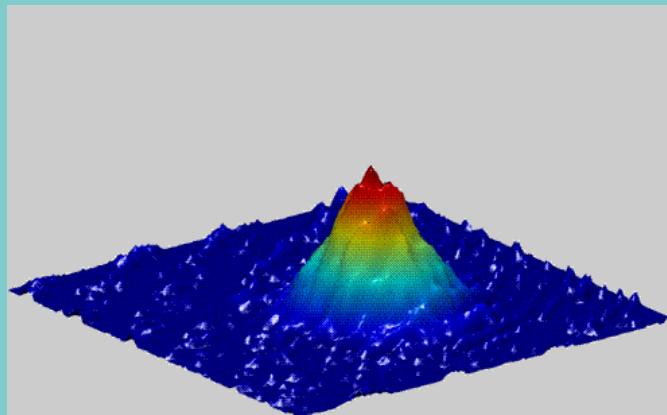
CO.CO.MAT

CONTROL OF QUANTUM CORRELATIONS IN TAILORED MATTER
SFB/TR 21 – STUTTGART, ULM, TÜBINGEN

Chromium BEC

BEC of Chromium atoms

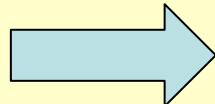
[Griesmaier et al., PRL 94, 160401 (2005)]



Also experiments on
Chromium in Paris-Nord

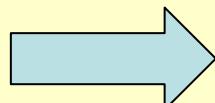
It is NOT just another BEC, because ...

Chromium has a large magnetic moment, $\mu=6\mu_B$



First available dipolar BEC

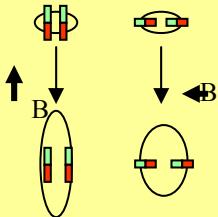
The ground state of ^{52}Cr is $^7\text{S}_3$



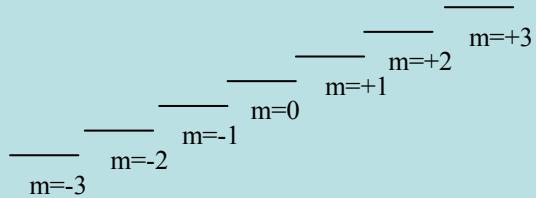
First available spin-3 BEC

Outline of the talk

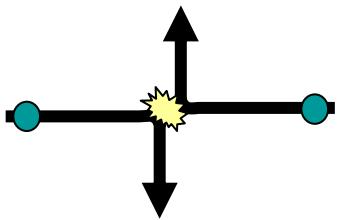
Dipolar gases



Cr-BEC as spin-3 BEC

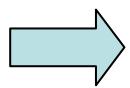
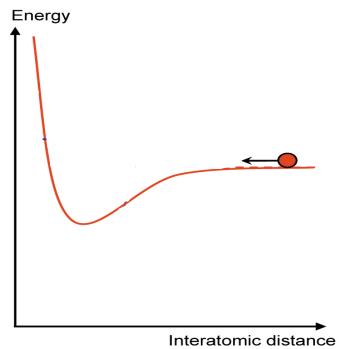


Dipolar gases



In typical experiments up to now the atoms interact via short-range isotropic interactions

The interaction is given by the s-wave scattering length “a”



$$V(\vec{r} - \vec{r}') \approx \frac{4\pi\hbar^2 a}{m} \delta(\vec{r} - \vec{r}')$$

Dipolar gases

Recent experimental developments open a novel research area in cold gases:
the analysis of dipolar gases

Atoms with large magnetic moment, as Cr [Griesmaier et al.,
PRL **94**, 160401 (2005)]

Polar molecules

Direct cooling of polar molecules [Bethlem and Meijer, Int. Rev.
Phys. Chem. **22**, 73 (2003)]

Photoassociation of polar
molecules in optical lattices [Jaksch et al., PRL **89**, 040402 (2002);
Damski et al., PRL **90**, 110401 (2003);
Rom et al., PRL **93**, 073200 (2004)]

Feshbach resonances in
binary mixtures [Stan et al. PRL **93**, 143001 (2004);
Inouye et al., PRL **93**, 183201 (2004);
Petrov et al., cond-mat/0502010]

Laser induced dipole-dipole interaction [O'Dell et al., PRL **84**, 5687 (2000)]

Rydberg atoms [Jaksch et al., PRL **85**, 2208 (2000)]

Dipolar gases

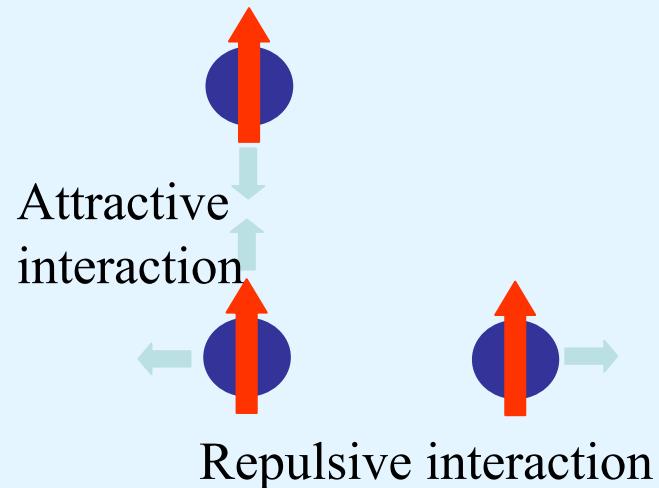
Dipole-dipole interaction



$$V(\vec{r}) = \frac{d^2}{r^3} (1 - 3 \cos^2 \theta)$$

The interaction is anisotropic
(partially attractive and
partially repulsive!)

Long-range interaction



Dipolar gases

At low temperatures the physics of a dipolar BEC is given by a nonlocal nonlinear Schrödinger equation

Nonlocal NLSE

$$i\hbar \frac{\partial}{\partial t} \psi(\vec{r}, t) = \left\{ \begin{array}{l} \frac{-\hbar^2}{2m} \nabla^2 + V(\vec{r}, t) + g |\psi(\vec{r}, t)|^2 + \\ + g_d \int d\vec{r}' \frac{(1 - 3 \cos^2 \theta)}{|\vec{r} - \vec{r}'|^3} |\psi(\vec{r}', t)|^2 \end{array} \right\} \psi(\vec{r}, t)$$

$$g \propto a \quad \longleftrightarrow \quad g_d \propto d^2$$

Nonlocal nonlinearity is also observed in other physical systems

Plasma physics

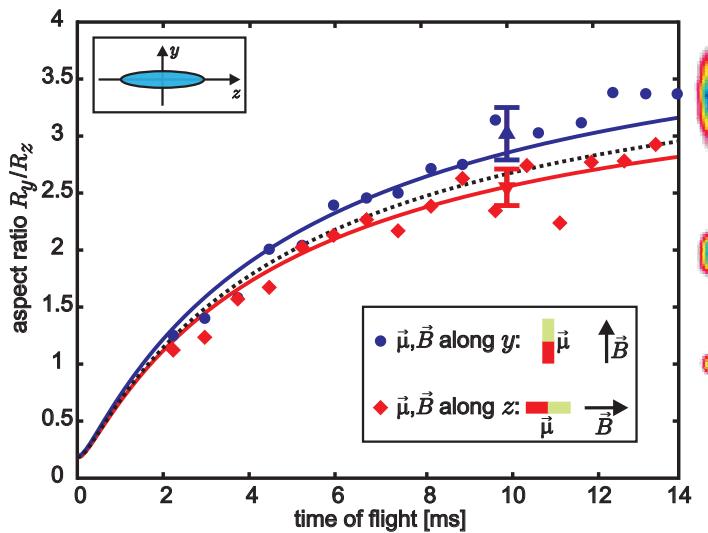
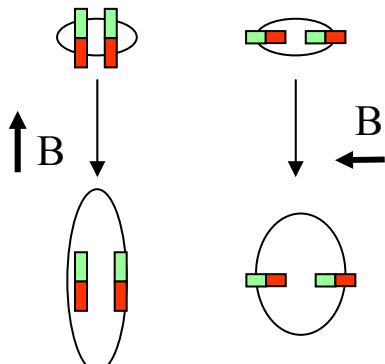
[Litvak et al., Sov. J. Plasma Phys. **1**, 60 (1975)]

Nematic Liquid Crystals

[Peccianti et al., Nature **432**, 733 (2004)]

The expansion dynamics of a dipolar BEC is significantly affected by the dipolar interaction

[Góral and Santos, PRA **66**, 023613 (2002); Yi and You, PRA **67**, 045601 (2003); Giovanazzi *et al.*, J. Opt. B **5**, 208 (2003)]



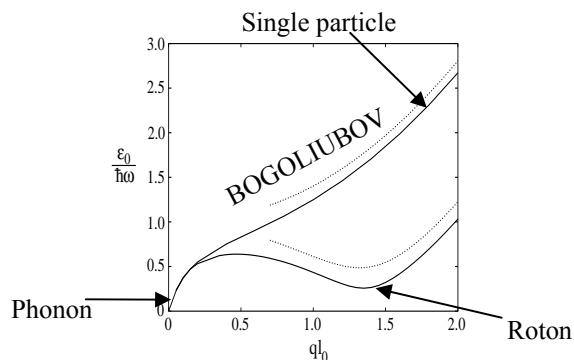
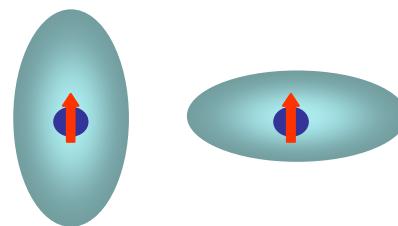
**First trace of
dipolar effects in
BEC ever!!**

Dipolar gases

Dipolar BEC presents many novel characteristic features

Trap-dependent stability

[Yi and You, PRA **61**, 041604 (2000);
Góral et al., PRA **61**, 051601 (2000);
Santos et al., PRL **85**, 1791 (2000)]



Roton-maxon excitation spectrum

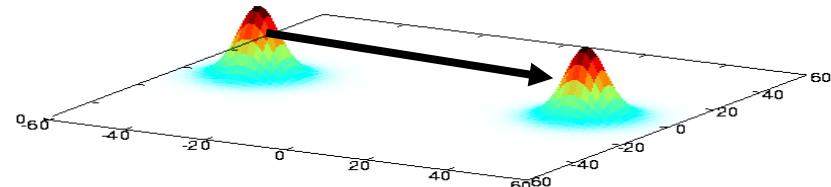
[O'Dell et al., PRL **90**, 110402 (2003);
Santos et al., PRL **90**, 250403 (2003)]

2D solitons

[Pedri and Santos,
PRL **95**, 150406 (2005)]

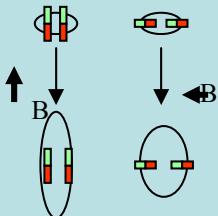
Inelastic scattering

Truly-2D motion without distortion!!

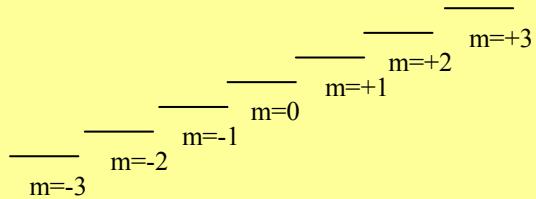


Outline of the talk

Dipolar gases



Cr-BEC as spin-3 BEC



Chromium BEC as a spinor BEC

Spin $\frac{1}{2}$ $|F = 1, m_F = -1\rangle$
 $|F = 2, m_F = +1\rangle$

Magnetically trapped ^{87}Rb

[Hall et al., PRL **81**, 1539 (1998)]

Spinor BEC

Spin 1 $|F = 1, m_F = \pm 1, 0\rangle$

Optically trapped

Na

[Stenger et al., Nature
396, 345 (1998)]

^{87}Rb

[Schmalljohann et al., PRL **92**,
040402 (2004);
Chang et al., PRL **93**, 170402
(2004);
Higbie et al., PRL **95**, 050401
(2005)]

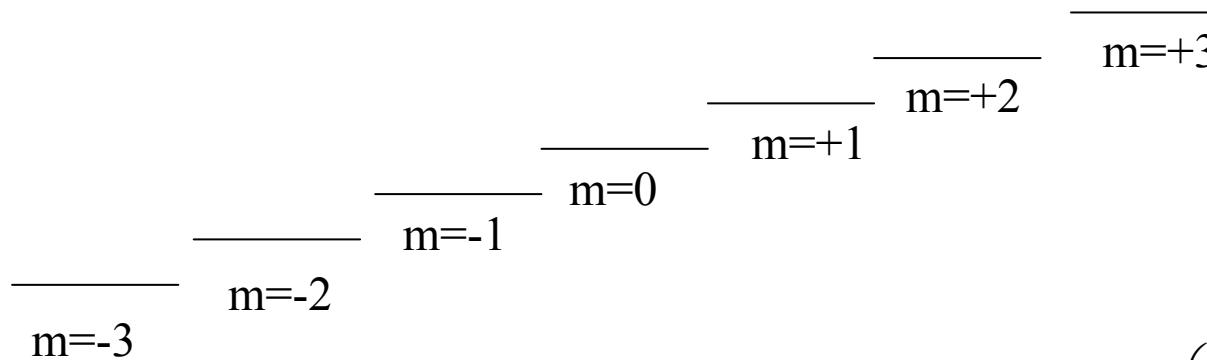
Spin 2 $|F = 2, m_F = \pm 2, \pm 1, 0\rangle$
 ^{87}Rb

[Schmalljohann et al., PRL **92**, 040402 (2004);
Kuwamoto et al., PRA **69**, 063604 (2004);
Widera et al., PRL **95**, 190405 (2005)]

Chromium BEC as a spinor BEC

[Santos and Pfau, cond-mat/0510634]

The ground state of ^{52}Cr is $^7\text{S}_3$



Hence, unless we pump into one state (which is what is done up to now), we will have to deal with a **spinor wavefunction with 7 components !!!**

$$\vec{\psi} = \begin{pmatrix} \psi_{-3} \\ \psi_{-2} \\ \psi_{-1} \\ \psi_0 \\ \psi_{+1} \\ \psi_{+2} \\ \psi_{+3} \end{pmatrix}$$

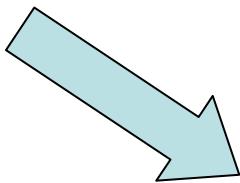
Spin-3 BEC

Chromium BEC as a spinor BEC

Hamiltonian

$$\hat{H} = \hat{H}_0 + \hat{V}_{sr} + \hat{V}_{dd}$$

Single particle physics Short-range interactions Dipole-dipole interactions



$$\hat{H}_0 = \int d\vec{r} \sum_m \hat{\psi}_m^+(\vec{r}) \left[\frac{-\hbar^2}{2M} \nabla^2 + U_{trap}(\vec{r}) + pm \right] \hat{\psi}_m(\vec{r})$$

$$\text{Zeeman effect } p = g\mu_B B$$

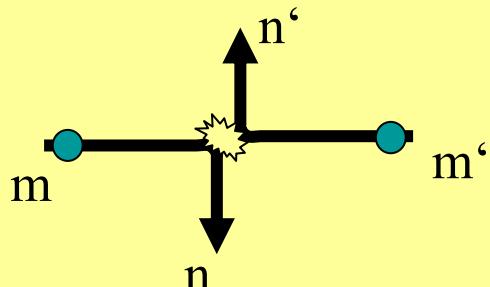
(No quadratic Zeeman effect in Cr-BEC)

Chromium BEC as a spinor BEC

Hamiltonian

$$\hat{H} = \hat{H}_0 + \hat{V}_{sr} + \hat{V}_{dd}$$

Single particle physics Short-range interactions Dipole-dipole interactions



$$\hat{V}_{sr} = \frac{1}{2} \int d\vec{r} \sum_S g_S \hat{P}_S(\vec{r})$$

[Ho, PRL 81, 742 (1998)]

They conserve the total spin : $S = m + m' = n + n'$

a_s s-wave scattering length for total spin S

Only even S is possible for Bosons: $S=0,2,4,6$

$$g_S = 4\pi\hbar^2 a_s / M$$

This is similar as for $S=2$, but having $S=3$ will lead to new physics!!

For ^{52}Cr :

[Werner et al., PRL 94, 183201 (2005)]

$$a_0 = ?$$

$$a_2 = -7(20)a_B$$

$$a_4 = 58(6)a_B$$

$$a_6 = 112(14)a_B$$

Chromium BEC as a spinor BEC

Hamiltonian

$$\hat{H} = \hat{H}_0 + \hat{V}_{sr} + \hat{V}_{dd}$$

Single particle physics Short-range interactions Dipole-dipole interactions

They do **NOT** conserve the total spin

$$\hat{V}_{dd} = \frac{c_d}{2} \int d\vec{r} \int d\vec{r}' \frac{1}{|\vec{r} - \vec{r}'|^3} \hat{\psi}_m^+(\vec{r}) \hat{\psi}_{m'}^+(\vec{r}') \left[\frac{S_{mn} \cdot S_{m'n'} -}{3(S_{mn} \cdot e)(S_{m'n'} \cdot e)} \right] \hat{\psi}_n(\vec{r}) \hat{\psi}_{n'}(\vec{r}')$$

This violation of the spin conservation means that
spin can be transferred into center-of-mass angular momentum!!

$S = (S_x, S_y, S_z)$ are the spin-3 matrices

$$e = (\vec{r} - \vec{r}') / |\vec{r} - \vec{r}'|$$

Chromium BEC as a spinor BEC: Ground state

Mean-field approximation $\hat{\psi}_m(\vec{r}) \cong \sqrt{N}\psi_m(\vec{r})$

Single-mode approximation $\psi_m(\vec{r}) = \Phi(\vec{r})\psi_m$

Magnetic field in z-direction

$$E[\langle\psi_m\rangle] \cong \tilde{p}\langle S_z \rangle + \tilde{c}_1\langle S_z \rangle^2 + \frac{4}{7}c_2|\Theta|^2 + c_3\left(\frac{3}{2}\langle S_z^2 \rangle^2 - 12\langle S_z^2 \rangle + \frac{1}{2}\langle S_+^2 \rangle^2 + 2\langle S_+S_z \rangle^2\right)$$

$$c_1 = (g_6 - g_2)/18 \approx 0.65g_6$$

$$c_2 = g_0 + (-55g_2 + 27g_4 - 5g_6)/33 \approx g_0 + 0.374g_6$$

$$c_3 = g_2/126 - g_4/77 + g_6/198 \approx -0.002g_6$$

$$\Theta = \frac{1}{2} \sum_m (-1)^m \psi_m \psi_{-m}$$

$$\tilde{p} = 2p/N \int d\vec{r} |\Phi(\vec{r})|^4$$

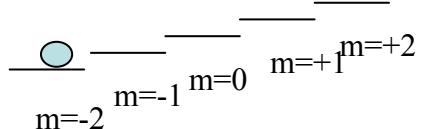
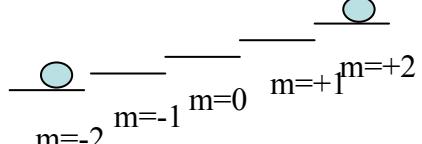
Chromium BEC as a spinor BEC: Ground state

In order to get a feeling, let's compare with spin-2 BEC

[Ciobanu et al., PRA 61, 033607 (2000);
Koashi and Ueda, PRL 84, 1066 (2000)]

$$E \cong \tilde{p} \langle S_z \rangle + c_1 \langle S_z \rangle^2 + \frac{4}{5} c_2 |\Theta|^2$$

The same but without
the c_3 term !!

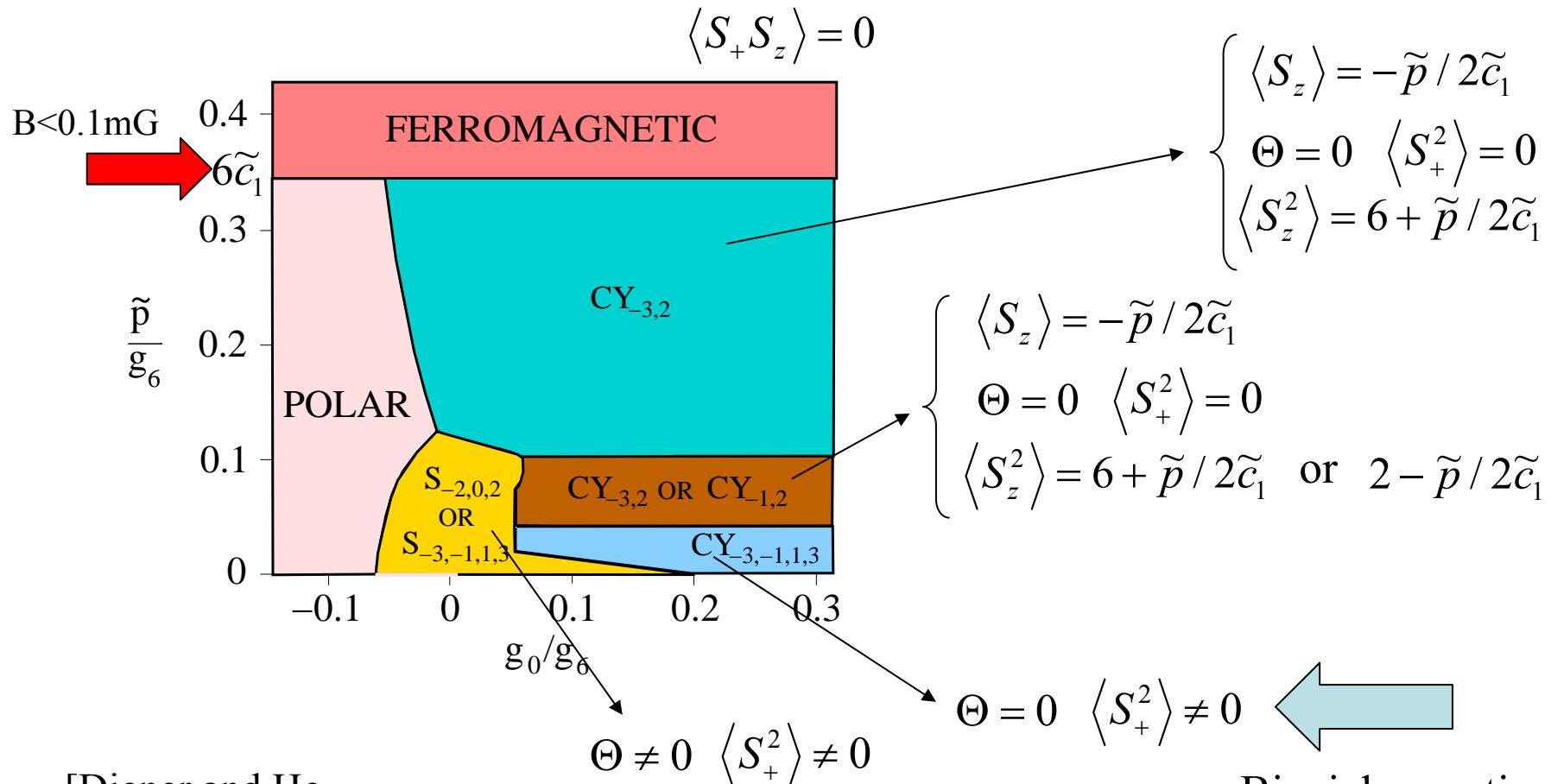
Ferromagnetic	$\Theta = 0$ $\langle S_z \rangle = 2$	$c_1 \leq \tilde{p} / 4$ $c_1 - c_2 / 20 \leq \tilde{p} / 4$	
Polar ⁸⁷ Rb	$\Theta \neq 0$	$c_2 < 0$ $c_1 - c_2 / 20 > \tilde{p} / 4$	
Cyclic	$\Theta = 0$ $\langle S_z \rangle \neq 2$	$c_2 > 0$ $c_1 > \tilde{p} / 4$	Relative phases important

For spin-1: only ferromagnetic (⁸⁷Rb) or polar (Sodium)

[Ho, PRL **81**, 742 (1998)]

Chromium BEC as a spinor BEC: Ground state

$$E[\{\psi_m\}] \approx \tilde{p}\langle S_z \rangle + \tilde{c}_1\langle S_z \rangle^2 + \frac{4}{7}c_2|\Theta|^2 + c_3\left(\frac{3}{2}\langle S_z^2 \rangle^2 - 12\langle S_z^2 \rangle + \frac{1}{2}\langle S_+^2 \rangle^2 + 2\langle S_+S_z \rangle^2\right)$$



[Diener and Ho,
cond-mat/0511751]

[Madsen et al., PRL 92, 45505 (2004);
Acharya et al., PRL 92, 145506 (2004)]

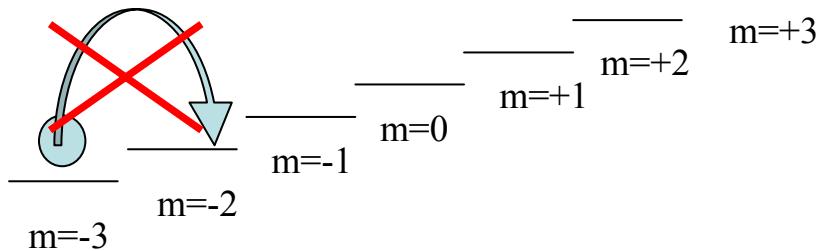
Chromium BEC as a spinor BEC: Dynamics

The dipole-dipole interaction plays a little role in the ground-state properties

But it can play a crucial role in the dynamics!

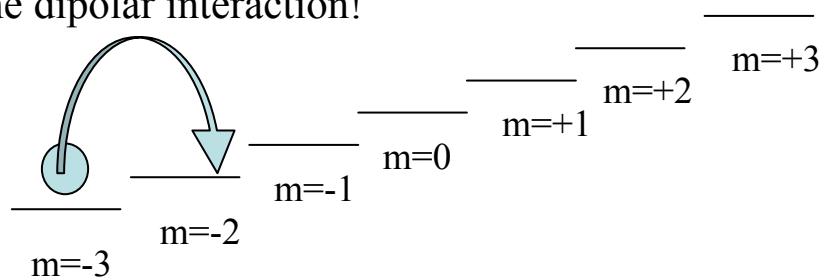
Only short-range part

Forbidden by
spin-conservation



With dipolar interaction

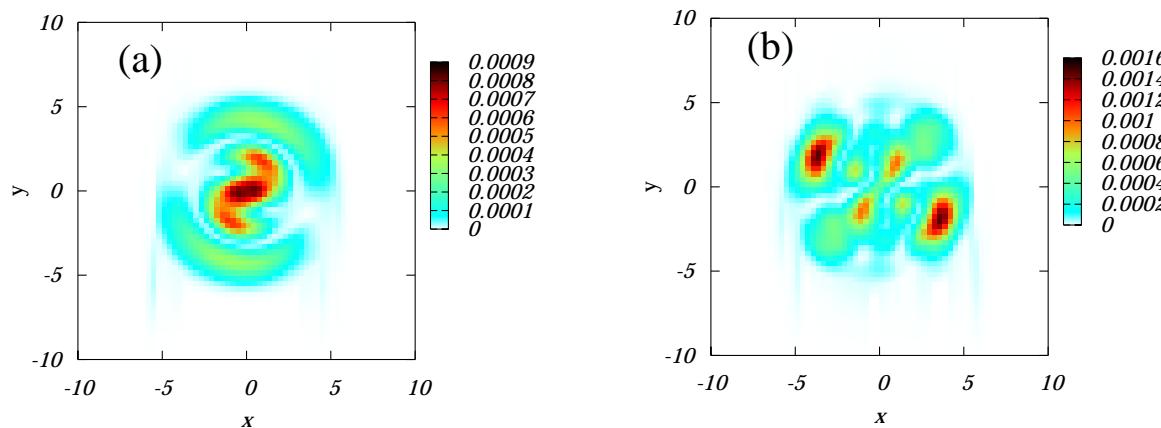
Spin-relaxation due to
the dipolar interaction!



The loss in spin, must be gained by the center of mass angular momentum

Chromium BEC as a spinor BEC: Dynamics

Density for the state $m=-2$



The state $m=-2$ starts to rotate!

It resembles the Einstein-de Haas effect

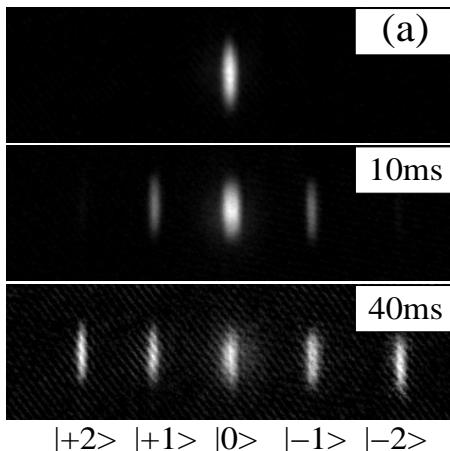
[Kawaguchi et al., cond-mat/0511052]

The coherent EH-effect is destroyed if $g\mu_B B \gg \hbar\omega$

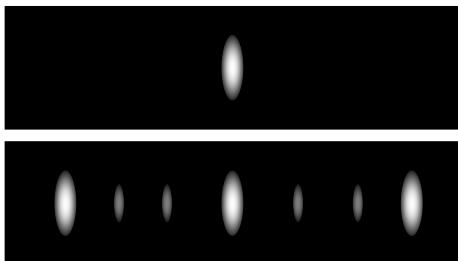
Chromium BEC as a spinor BEC: Dynamics

Also the c_3 terms have a significant role in the spinor dynamics and may lead to a rapid transfer from $m=0$ to $m=+3$ and $m=-3$

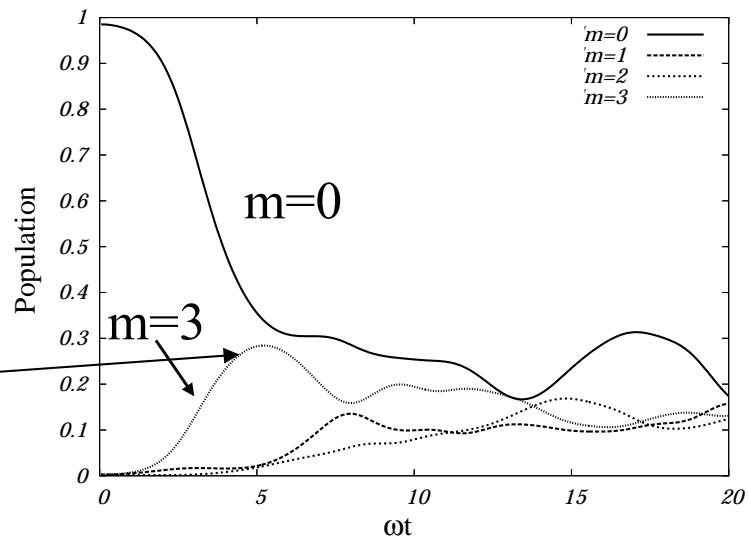
^{87}Rb



[Schmalljohann et al., PRL **92**, 040402 (2004)]

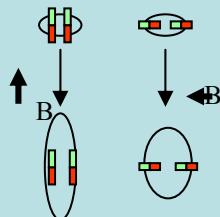


For $F=2$ a sequential population is observed

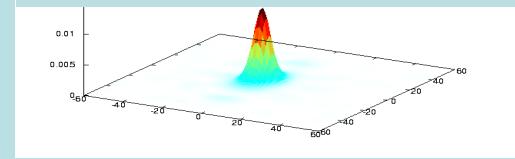


Summary

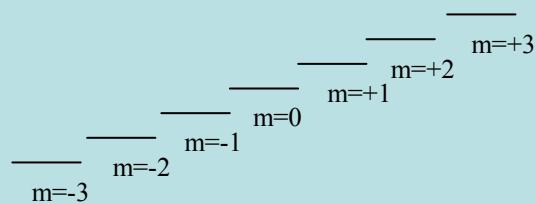
Properties of Dipolar BECs



Nonlocal nonlinearity. Multidimensional solitons



Cr-BEC as spinor BEC



1D Dipolar gases

[Sinha and Santos, in preparation)]

Dipolar Lattice gases

[Góral et al., PRL **88**, 170406 (2002)]

Fermionic dipolar gases [Baranov et al., PRL **92**, 250403 (2004)]

Rotating dipolar gases [Baranov et al., PRL **94**, 070404 (2005); Rezayi et al., cond-mat/0507064]

Quantum information [Brennen et al., PRL **82**, 1060 (1999); Jaksch et al., PRL **85**, 2208 (2000); DeMille et al., PRL **88**, 067901 (2002)]

People



P. Pedri

S. Sinha

S. Giovanazzi

R. Nath

L. Santos

J. Stuhler

A. Griesmaier

T. Koch

M. Fattori

T. Pfau

M. Baranov, B. Damski, K. Góral, M. Lewenstein,
E. Tiemann, G. V. Shlyapnikov, S. Kotochigova
P. Julienne, P. Zoller