

# Experiments with a high visibility lithium atom interferometer

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*Les Houches – February 2005*



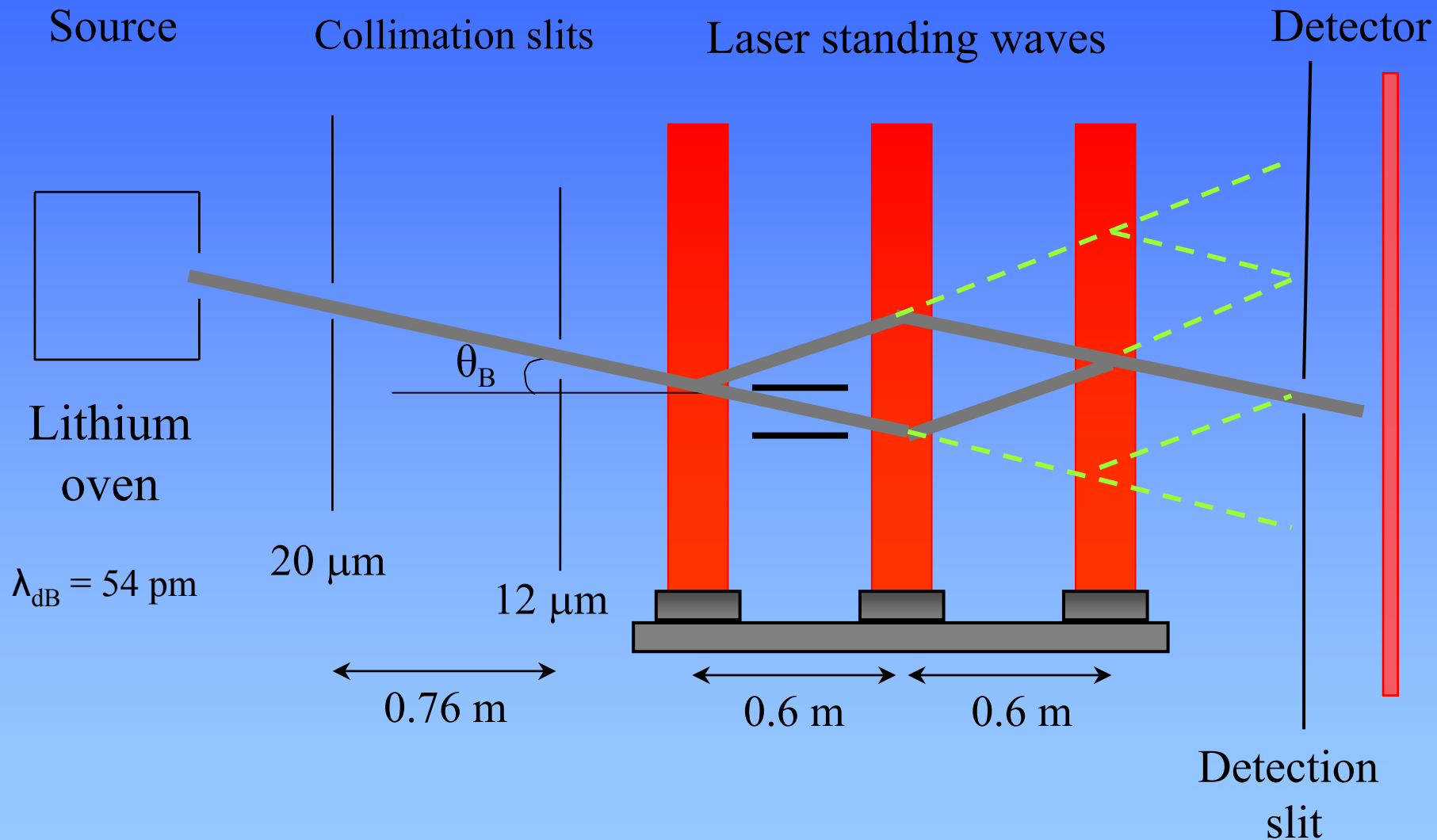
# Plan

I. Our atom interferometer

II. Experiments with a magnetic field gradient

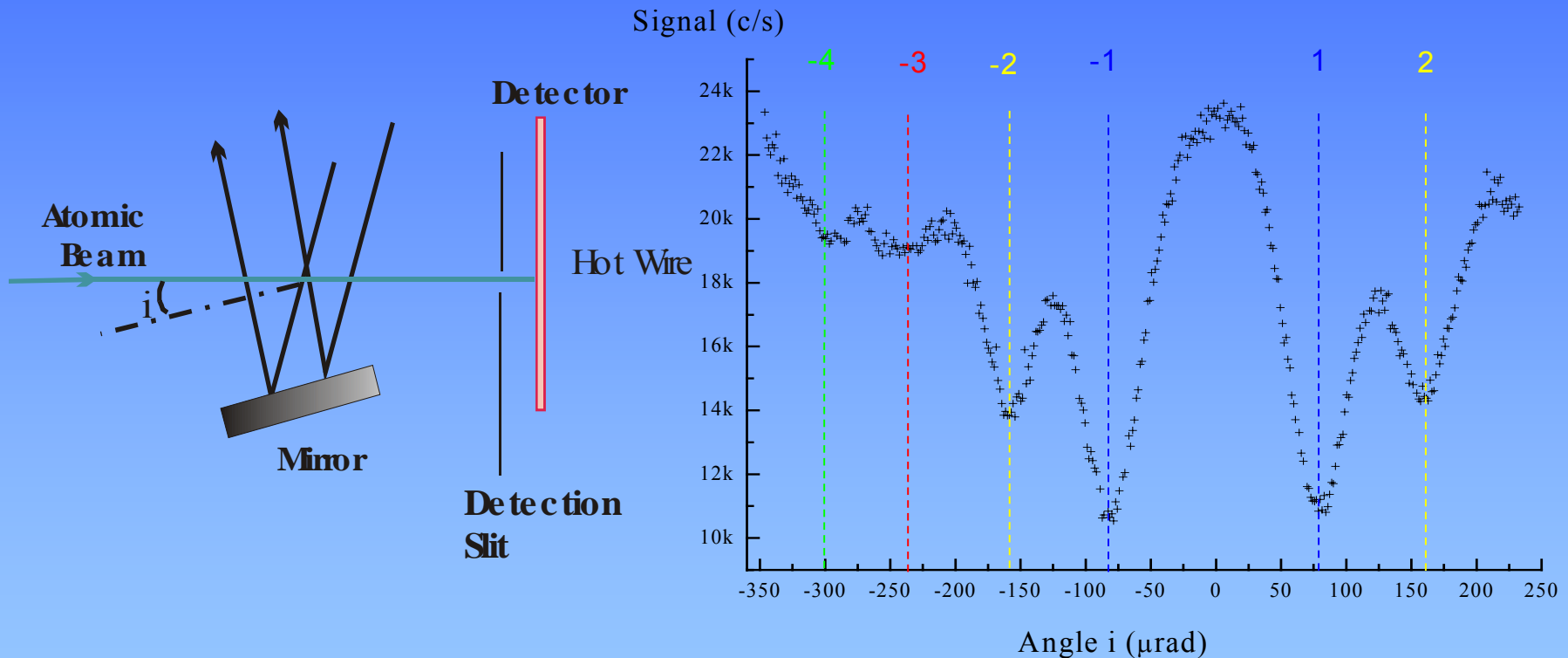
III. Lithium atom polarizability measurement

# Experimental set-up



# Diffraction of the lithium atomic wave

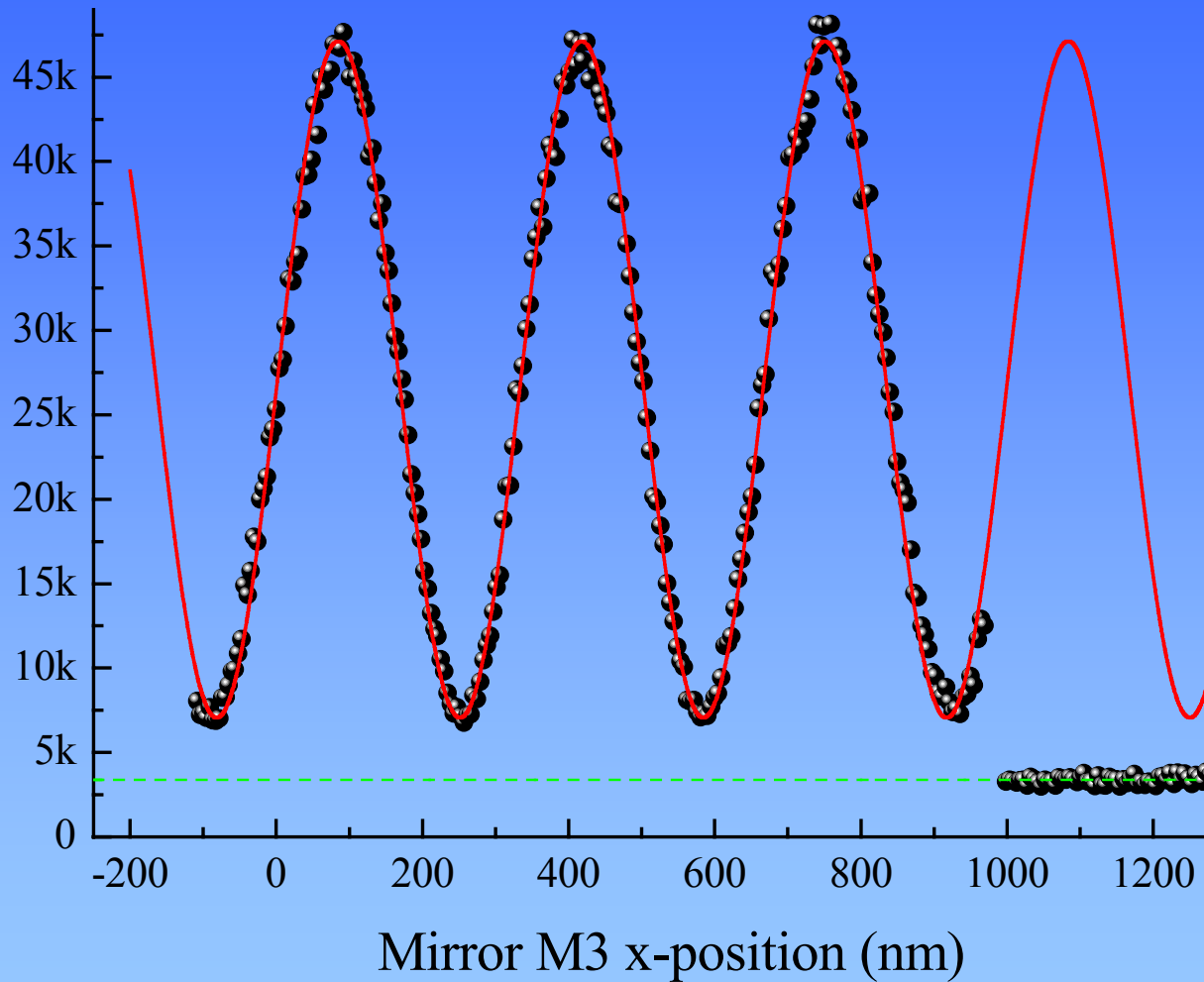
As a function of the orientation of the mirror used for the laser standing wave, the Bragg condition is fulfilled for various orders  $p$ , here from  $p = -2$  to  $p = +4$



Laser standing waves :  $\delta_L/(2\pi) = 1.2$  GHz,  $w_0 = 3.1$  mm,  $P_L = 240$  mW

# Lithium atom interference fringes

Signal (c/s)



**p = 1**

Fringe visibility  $V$   
 $= 84.5 \pm 1\%$

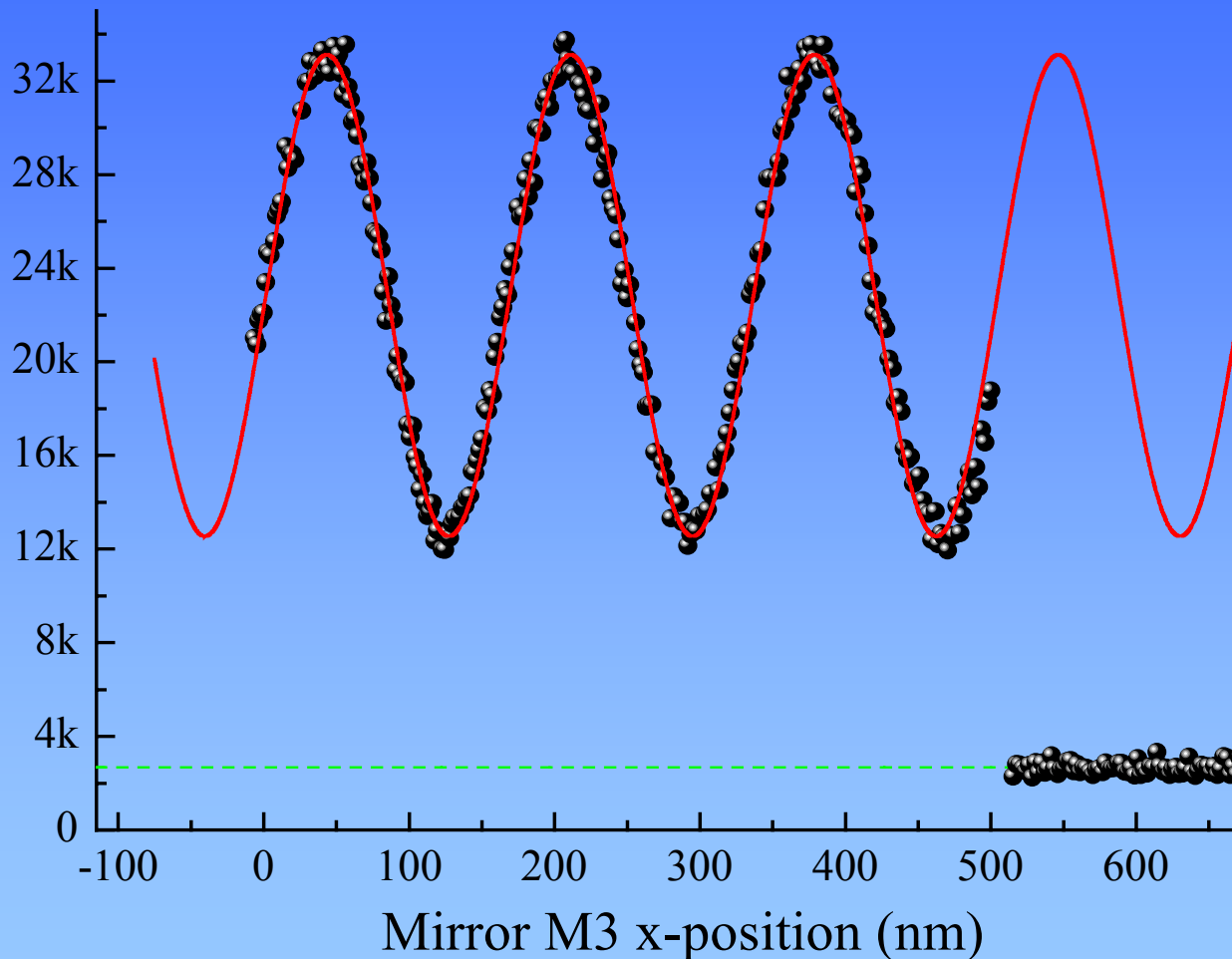
Output Flux  
 $I_0 = 23700$  c/s

Phase sensitivity  
 $25$  mrad /  $\sqrt{\text{Hz}}$

Laser standing waves:  $\delta/(2\pi) = 2.8$  GHz,  $w_0 = 5.0$  mm,  $P = 150$  mW

# Atom fringes using Bragg order 2 diffraction

Signal (c/s)



$p = 2$

Fringe visibility

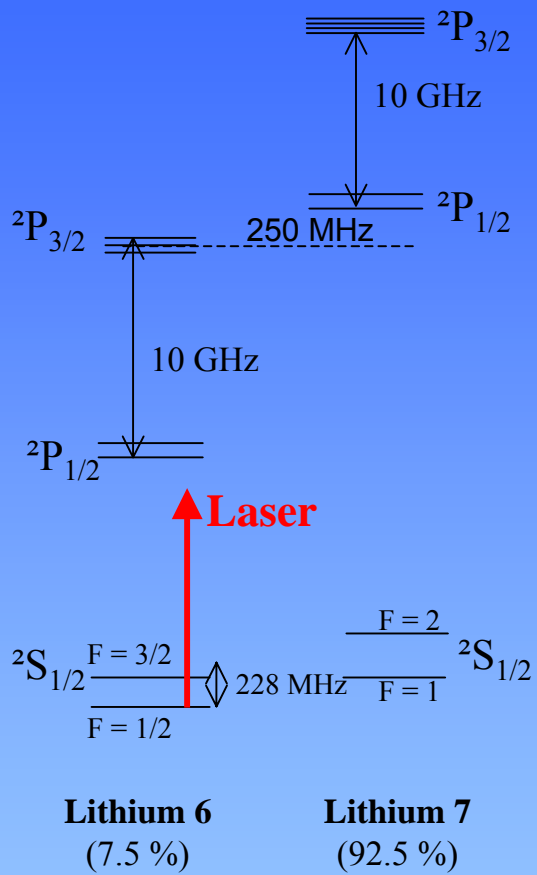
$$V = 54 \pm 1\%$$

Output Flux

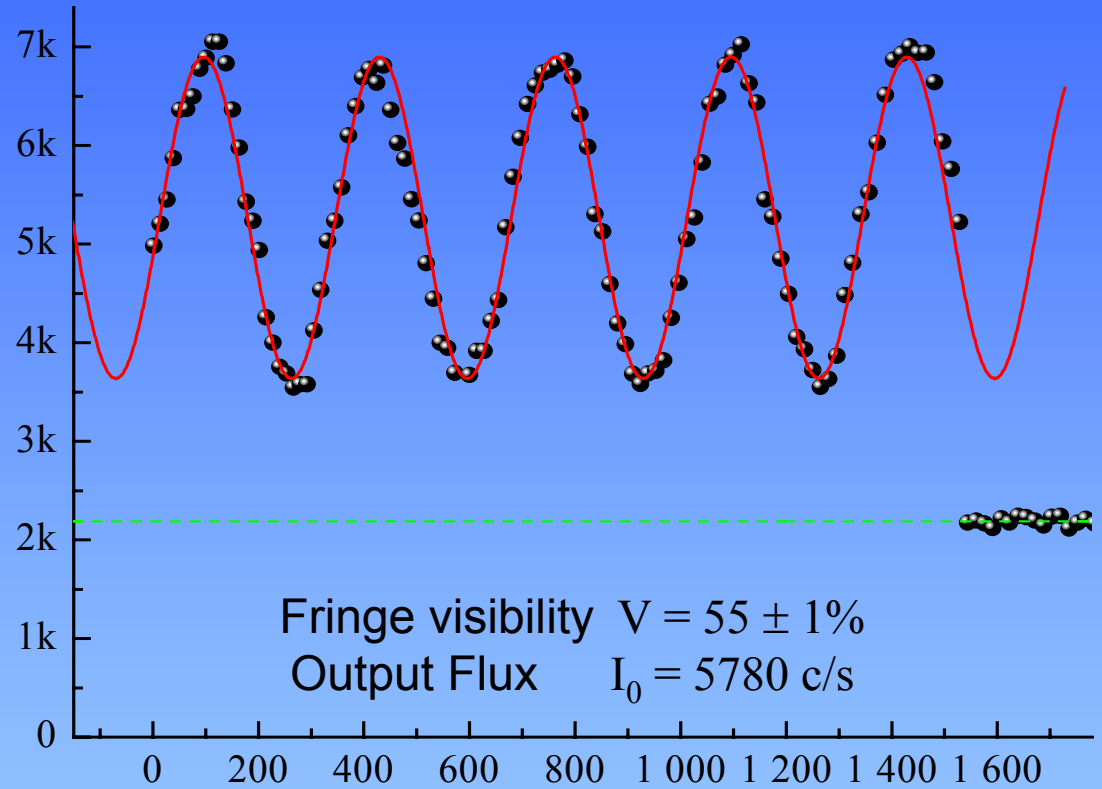
$$I_0 = 20180 \text{ c/s}$$

Laser standing waves:  $\delta/(2\pi) = 3.1 \text{ GHz}$ ,  $w_0 = 1.8 \text{ mm}$ ,  $P = 460 \text{ mW}$

# Isotope 6 interference fringes



Signal (kc/s)



Fringe visibility  $V = 55 \pm 1\%$   
 Output Flux  $I_0 = 5780 \text{ c/s}$

Mirror M3 - x position (nm)

## II. Experiments with a magnetic field gradient

- The  $|F, M_F\rangle$  sublevels are the eigenstates
- Adiabatic approximation

The magnetic field  $B$  does not vanish or rotate too rapidly

- Zeeman Phase Shift

$$\Delta\phi(F, M_F) = \varphi M_F$$

$$\varphi = \frac{g_F \mu_B}{\hbar v} \int \frac{dB(s)}{dx} \Delta x(s) ds$$

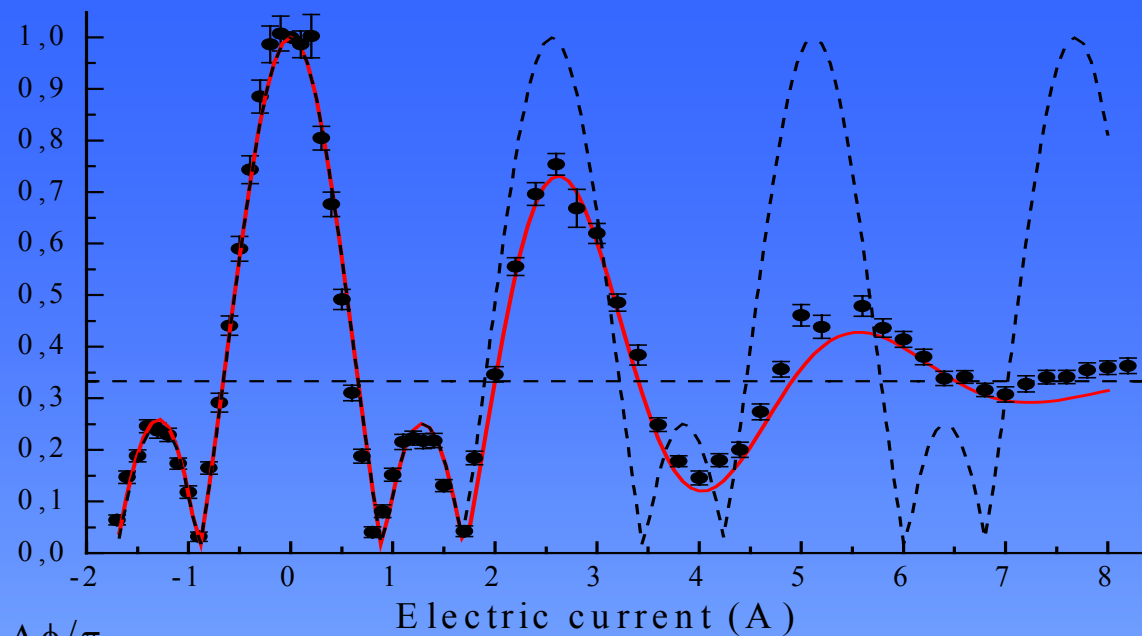
- For  ${}^7\text{Li}$  ( $I = 3/2$ ),  ${}^2\text{S}_{1/2}$ ,  $F=1$  and  $F=2 \rightarrow 8$  sublevels (Landé factors  $g_F = \pm 1/2$ )

Optical pumping in  ${}^2\text{S}_{1/2, F=1}$

$$\frac{V}{V_{MAX}} = \frac{1 + 2 \cos(\varphi)}{3}$$



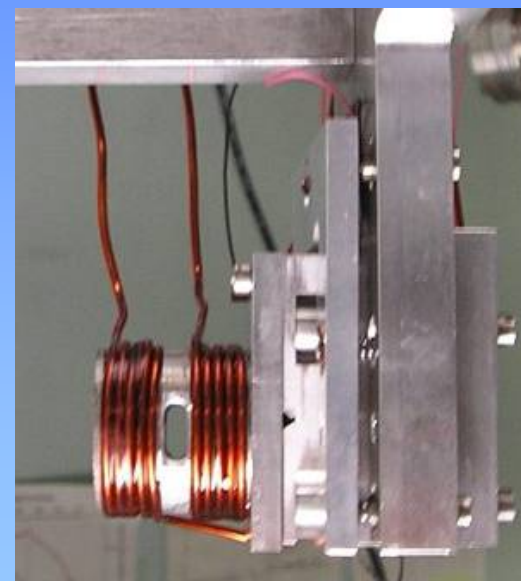
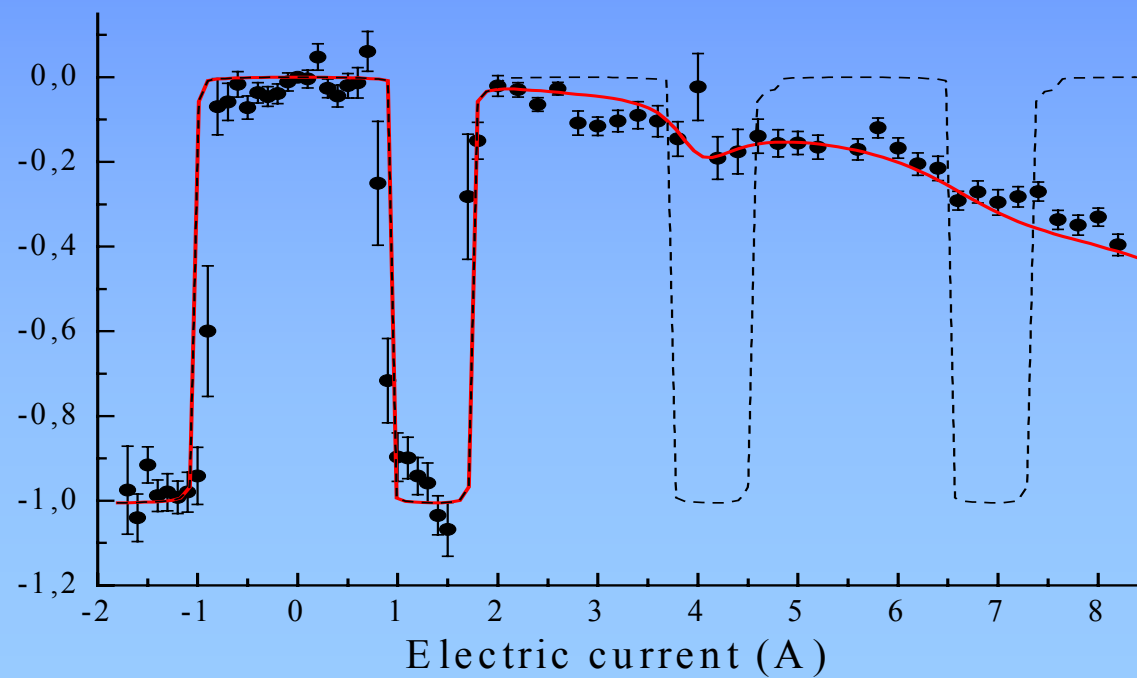
$V/V_{\text{Max}}$



----- Theoretical simulation without velocity dispersion

———— Theoretical simulation including velocity dispersion

$\Delta\phi/\pi$



# Magnetic rephasing experiment with ${}^6\text{Li}$ ( $I = 1$ )

$V/V_{\text{MAX}}$

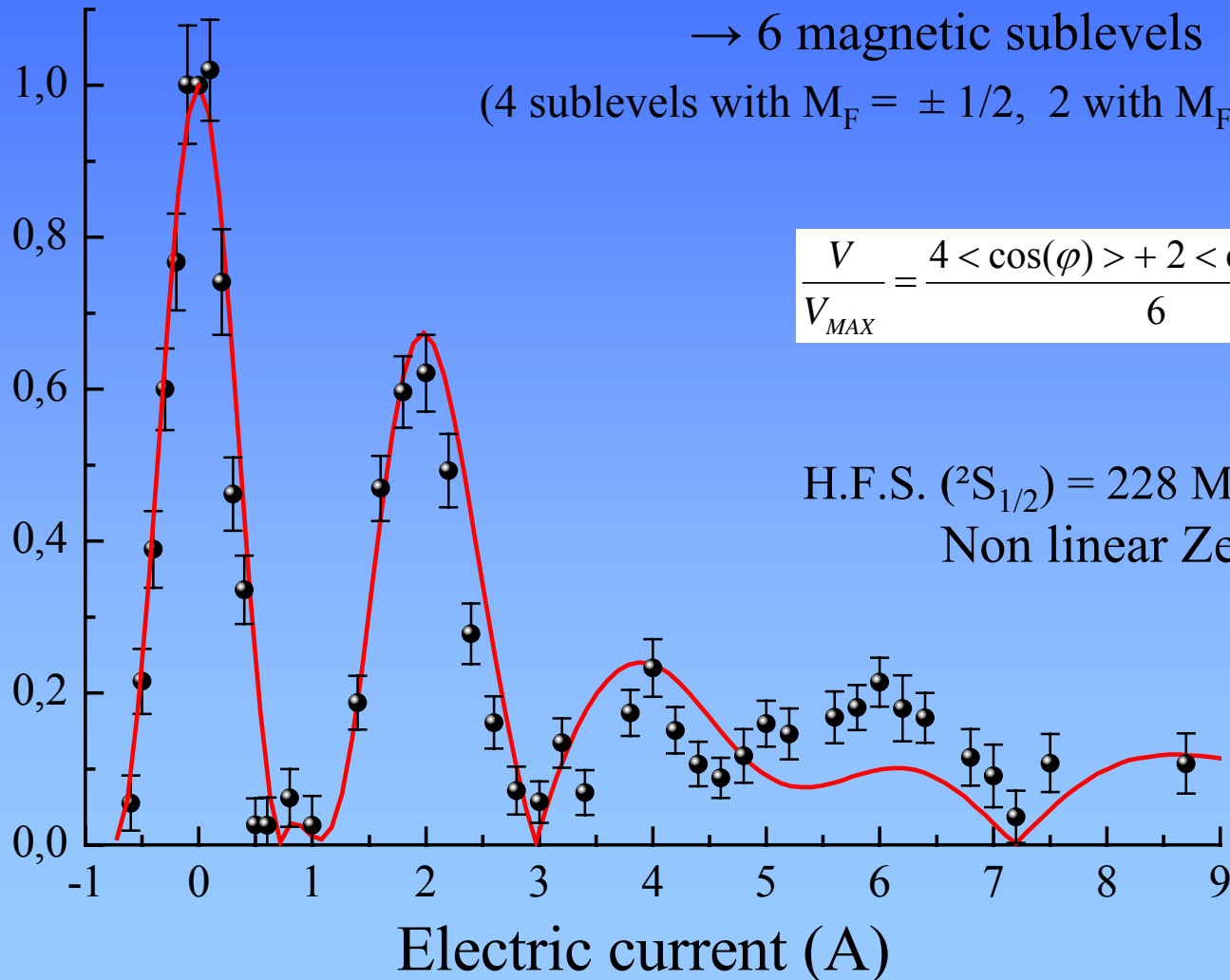
${}^2\text{S}_{1/2}$ ,  $F=1/2$  and  $F=3/2$  ( $g_F = \pm 1/3$ )

→ 6 magnetic sublevels

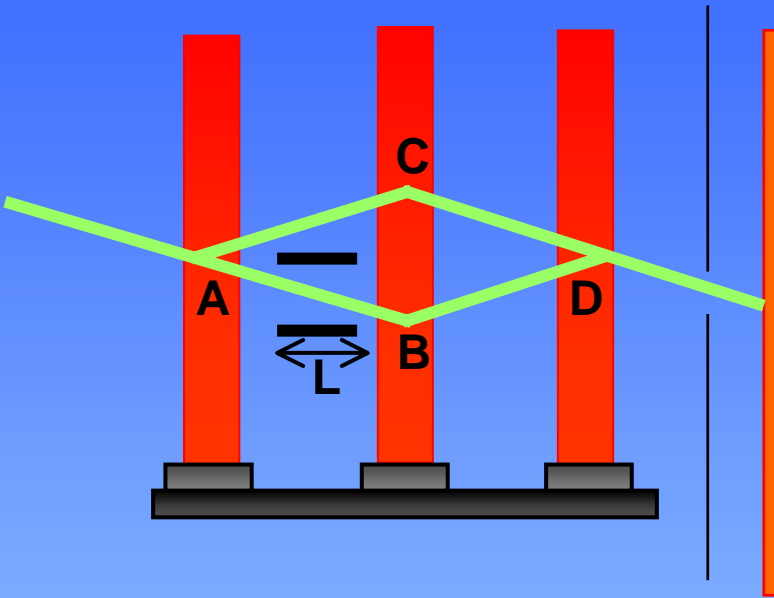
(4 sublevels with  $M_F = \pm 1/2$ , 2 with  $M_F = \pm 3/2$ )

$$\frac{V}{V_{\text{MAX}}} = \frac{4 \langle \cos(\varphi) \rangle + 2 \langle \cos(2\varphi) \rangle}{6}$$

H.F.S. ( ${}^2\text{S}_{1/2}$ ) = 228 MHz smaller than for  ${}^7\text{Li}$   
Non linear Zeeman effects !



# III. Lithium atom polarizability measurement



$$\Delta\Phi = \int_{ABD} U(t) dt / \eta - \int_{ACD} U(t) dt / \eta$$

$$U = \text{Perturbation} = -4\pi\epsilon_0\alpha E^2/2$$

D.E. Pritchard et al, Phys. Rev. A **51**, 3883  
Electric polarizability of sodium atom

**Stark Phase Shift**

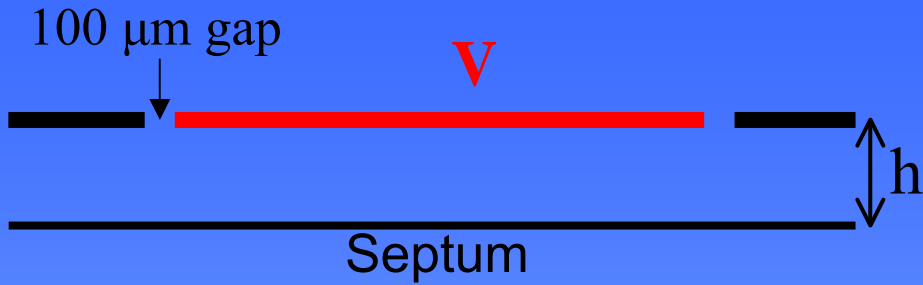
$$\Delta\phi_{\text{Stark}} = 4\pi\epsilon_0\alpha \frac{E^2 L}{2\eta\mu}$$

proportional to  $E^2/u$   
( $u$  = mean beam velocity)

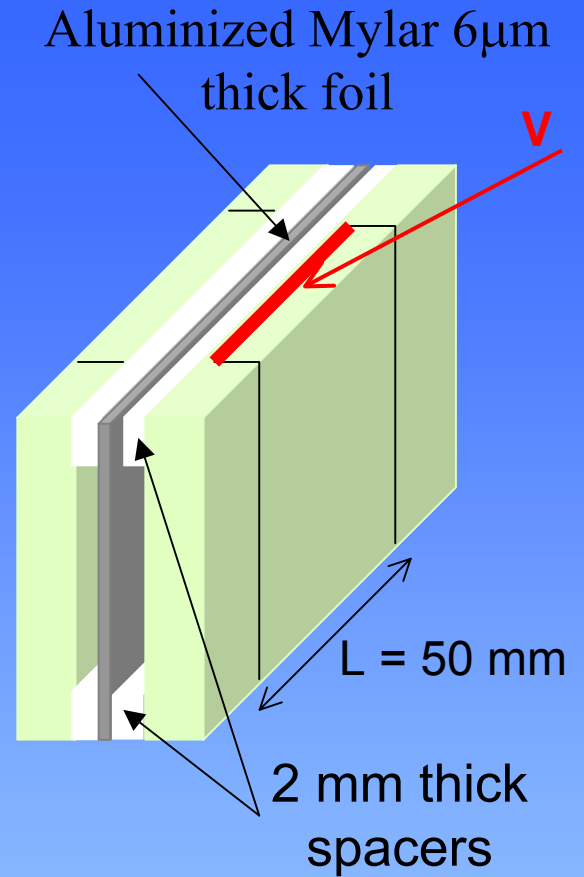
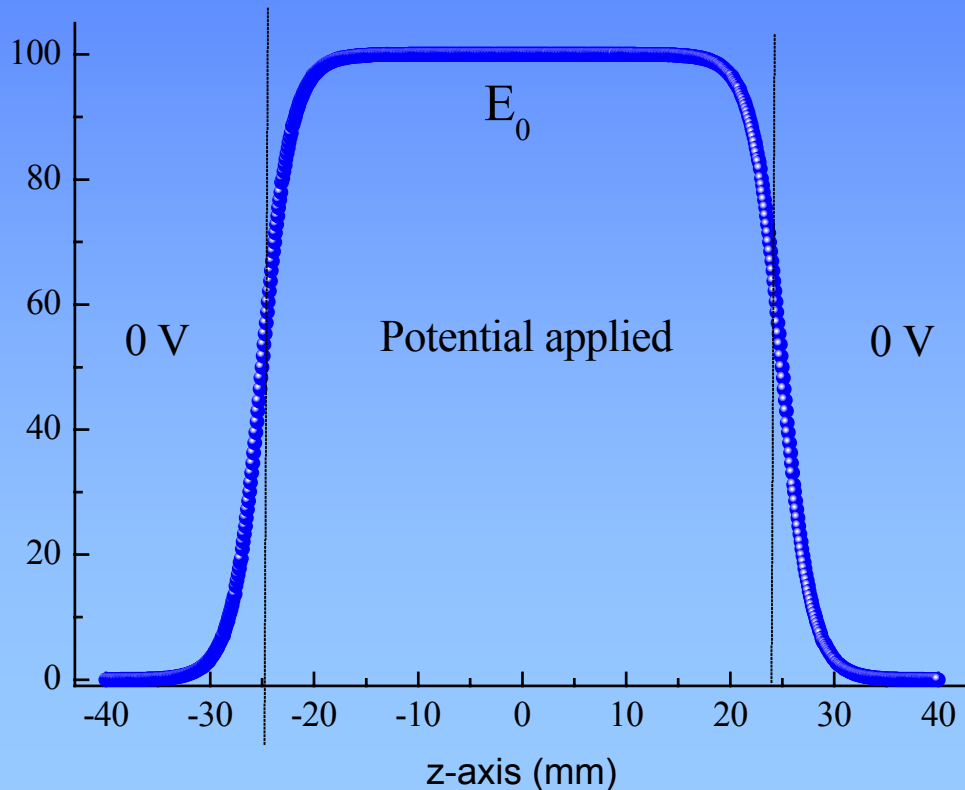
Two main difficulties :

1. Capacitor geometry, beam separation of 100 micrometers for  $p = 1$
2. Precise knowledge of the mean beam velocity of the atomic beam

# The capacitor built in Toulouse



Electric field  $E_x$  ( $\text{V}\cdot\text{mm}^{-1}$ )



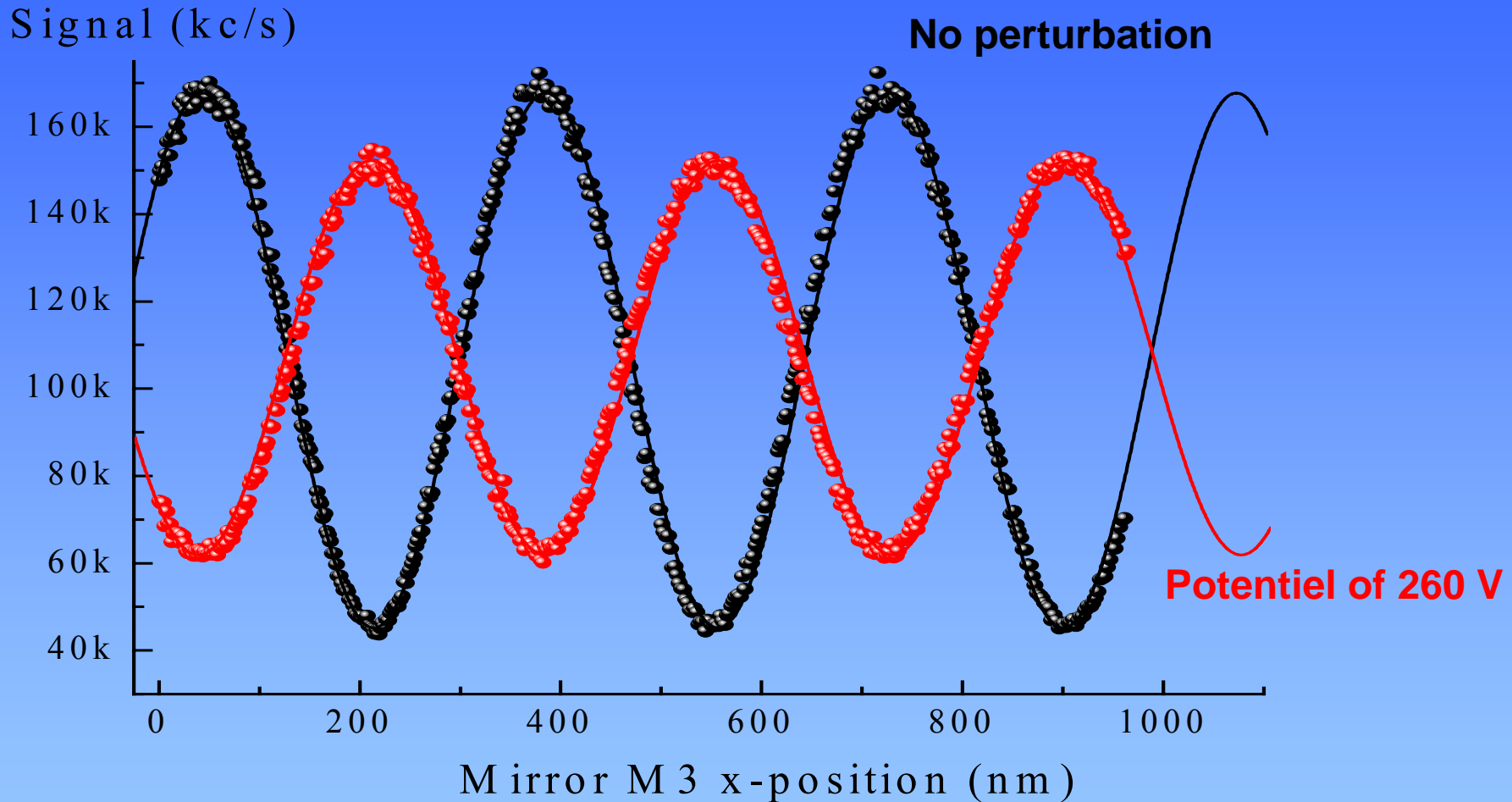
$$L_{\text{eff}} = \int E^2(z) dz / E_0^2$$

$$L_{\text{eff}} = 46,82 \pm 0,10 \text{ mm}$$

# Lithium atom polarizability

Error source	Systematic errors	
Effective length	$L_{\text{eff}} = 46,82 \pm 0,10 \text{ mm}$	0.21 %
Electrode spacing	$h = 2,027 \pm 0,002 \text{ mm}$	$2 \times 0.1 \%$
Contact potentials		0.01 %

# Observation of the phase Stark shift



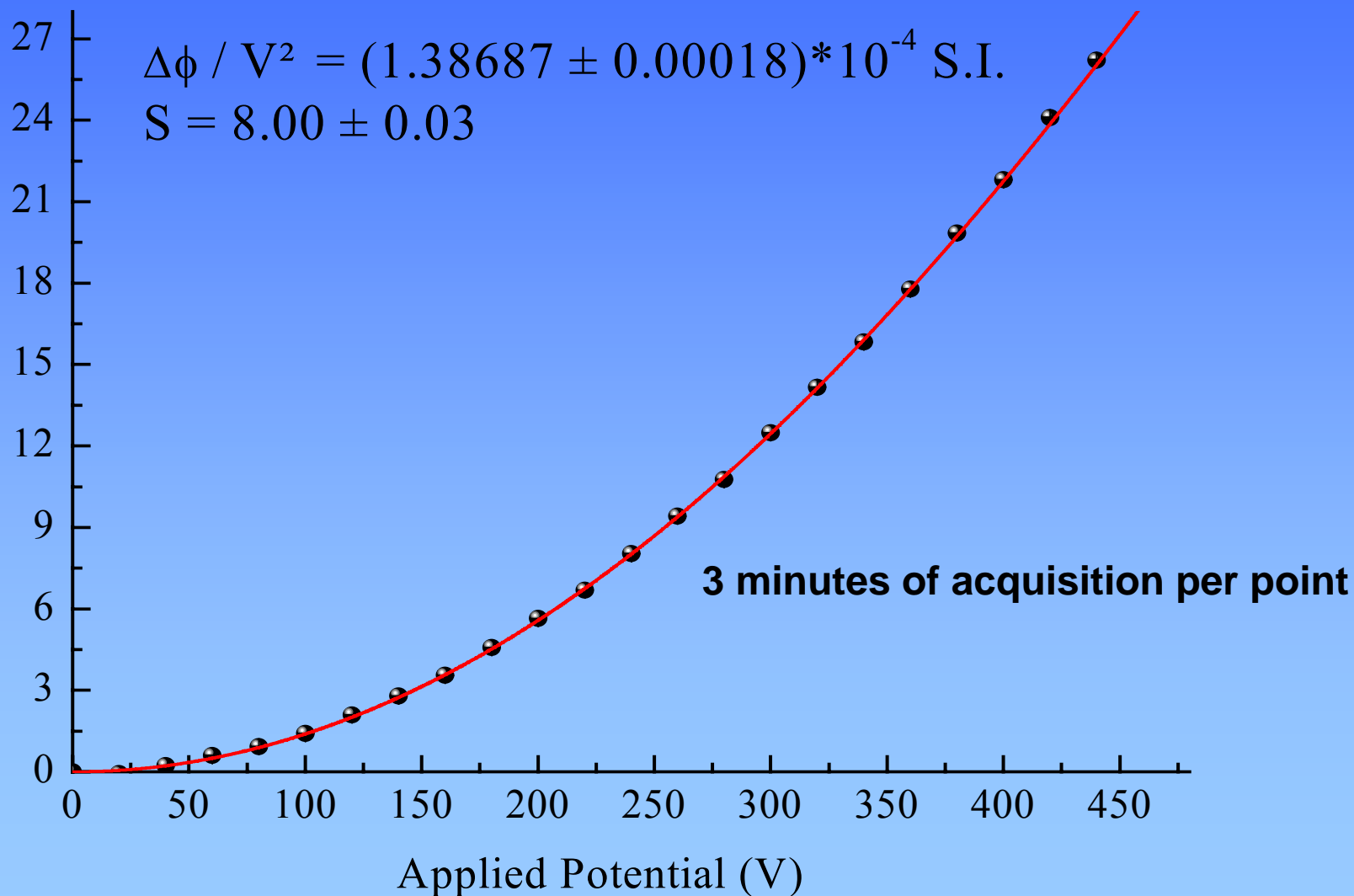
$$I_0 = 105\,000 \text{ c/s}$$
$$V_0 = 60\%$$

$$\Delta\Phi_{\text{Stark}} (260 \text{ V}) \sim 3\pi \text{ rad}$$

# Measurement of the phase shift

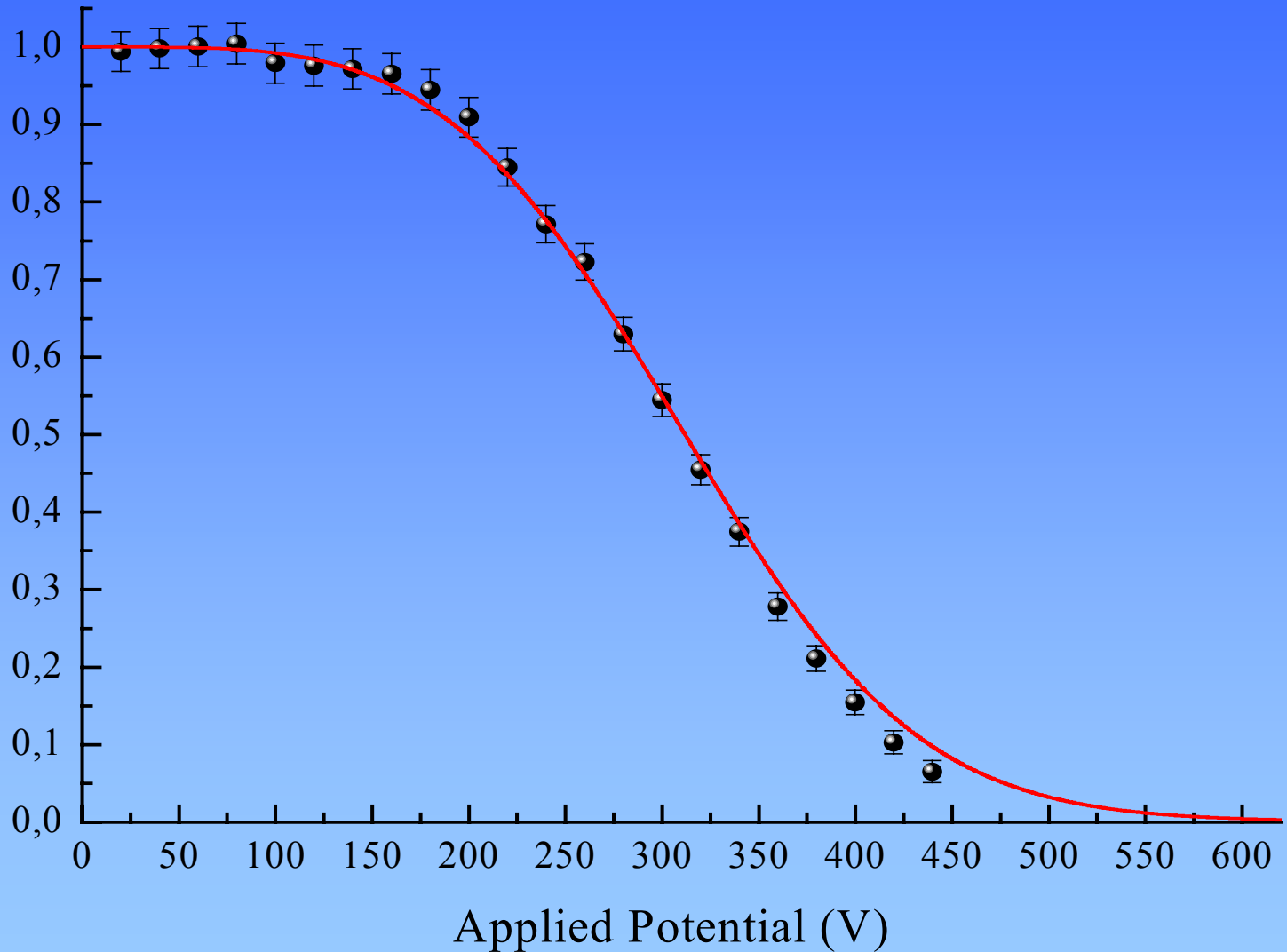
(Small corrections due to the velocity dispersion are included)

$\Delta\phi$  (rad)



# Fringe visibility as a function of the applied voltage

Fringe Visibility (normalized)



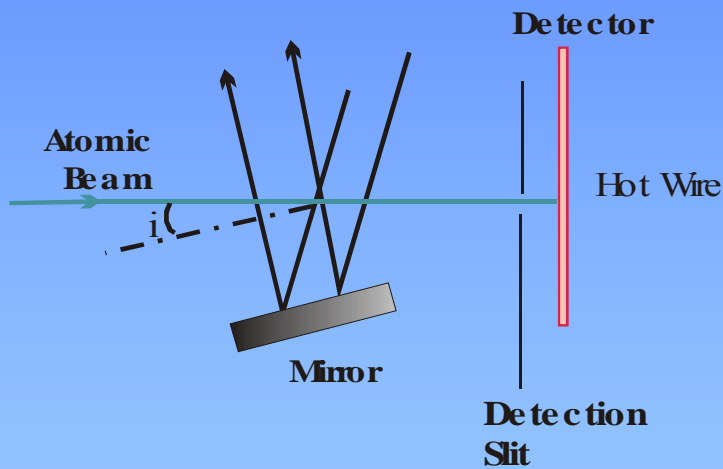


# Mean velocity of the atomic beam

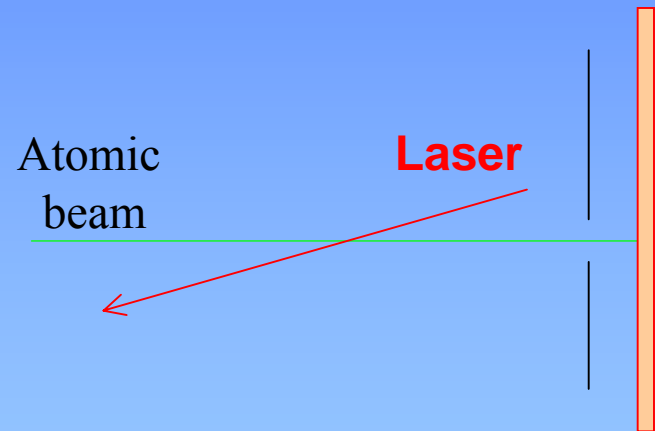
Two main methods

Bragg Diffraction

Doppler effect



$$u = 1075.7 \pm 5.4 \text{ m/s}$$



$$u = 1066.1 \pm 8.1 \text{ m/s}$$

# Lithium atom polarizability

Error source	Systematic errors	Statistical errors
Effective length	0.21 %	
Electrode spacing	$2 \times 0.1$ %	
Contact potentials	0.01 %	
Phase measurement		$\Delta\Phi/ V^2 = (1.38687 \pm 0.00018) \times 10^{-4}$ SI 0.1 %, analysis in progress
Velocity measurement		$u = 1073.1 \pm 7.0$ m/s    0.65 %

$$\alpha (\text{Li}) = 24,74 (8)_{\text{systematic}}(16)_{\text{statistical}} \times 10^{-30} \text{ m}^3$$

# Conclusions

## Atom interference fringes

High visibility and high flux,  
many possibilities (order 2, isotope 6)

## External fields as tools

- Internal structure of the atom, nuclear spin
- Lithium atom polarizability measurement

$$\alpha (\text{Li}) = 24,74 (8)_{\text{systematic}}(16)_{\text{statistical}} \times 10^{-30} \text{ m}^3$$

Our measurement ( $\sim 1\%$  accuracy) compares very well to the latest done by Molof et al. in 1974  $\alpha = (24,3 \pm 0,5) \times 10^{-30} \text{ m}^3$  (precision of 2%)

*A. Molof et al., Phys.Rev. A, 10, (1331-1140)*



# D. E Pritchard et al (1995) : Sodium atom electric polarizability

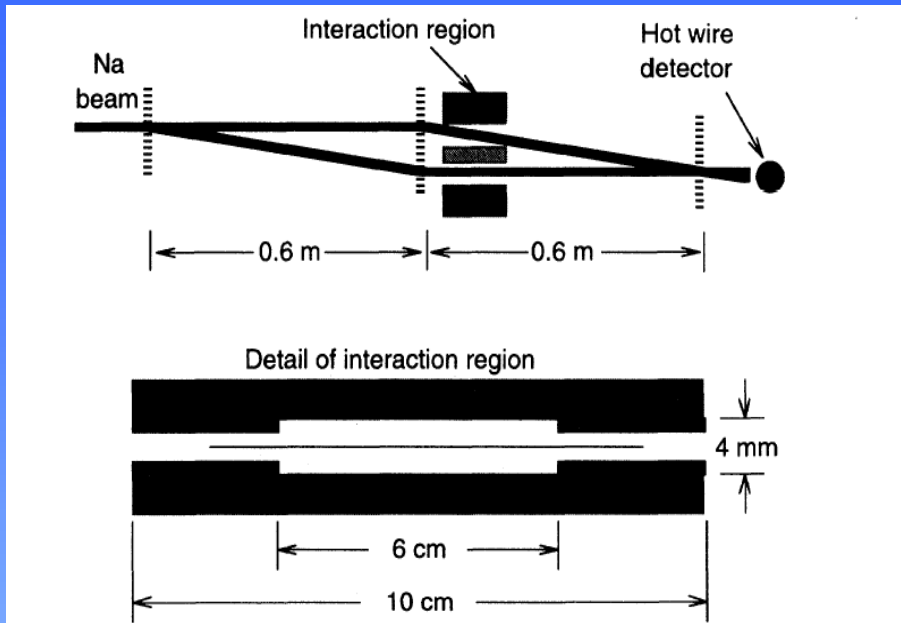


FIG. 1. Schematic of our interferometer and interaction region. Vertical dashed lines are 200-nm-period diffraction gratings. The detail of the interaction region shows the 10- $\mu\text{m}$  copper foil suspended between the side plates. The guard electrodes are indicated in black at both ends.

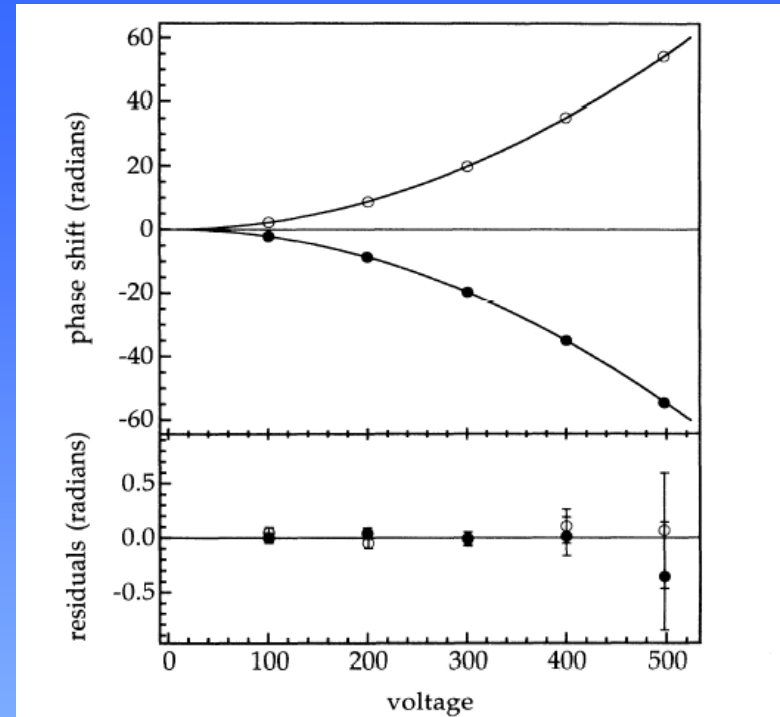


FIG. 5. Phase shift of the interference pattern as a function of voltage applied (in volts) to the left (open circles) or right (filled circles) side of the interaction region. The fit is to a quadratic and the residuals are shown in the lower graph.

$$U = -4\pi\epsilon_0\alpha E^2/2 \quad \rightarrow \quad \Delta\Phi \text{ proportional to } E^2/v$$

Accuracy on  $\alpha$  :  $\pm 0.25$  % statistical  $\pm 0.25$  % systematics

Main difficulties: capacitor geometry,  
precise knowledge of velocity distribution

# Index of refraction of gases for atomic waves

The index  $n$  is complex and expresses the effect of collisions.

$(n-1)$  is proportional to the gas density

$\text{Re}(n-1)$  measures the dephasing of the wave

$\text{Im}(n-1)$  measures the attenuation of the wave

Experiments with sodium by D. Pritchard et al.

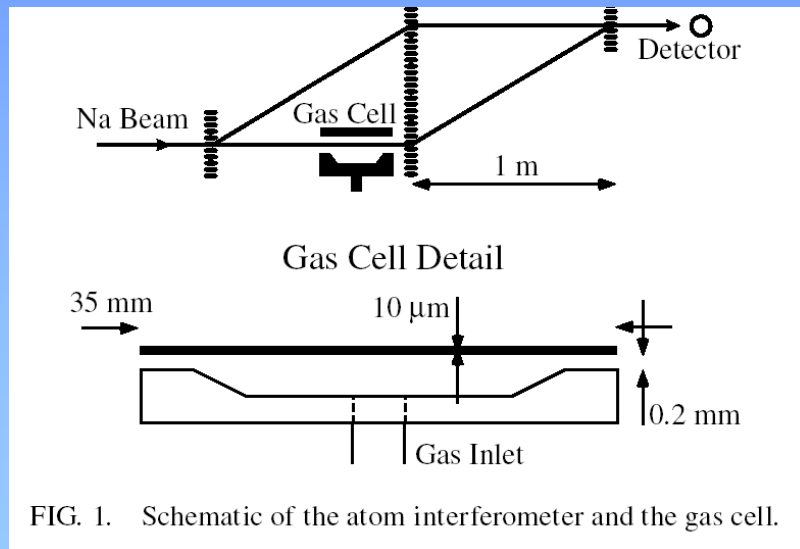


FIG. 1. Schematic of the atom interferometer and the gas cell.

$$\rho(v) = \frac{\text{Re}(n-1)}{\text{Im}(n-1)}$$

