

Non ideal trapped quantum gases

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Kioloa – dec 2004

Non ideal trapped quantum gases

1. Critical temperature shift in Rb
2. Penning ionization rate constants and scattering length in He*
3. Roughness of atom chip trapping potential

Non ideal
gas

Non ideal
trap

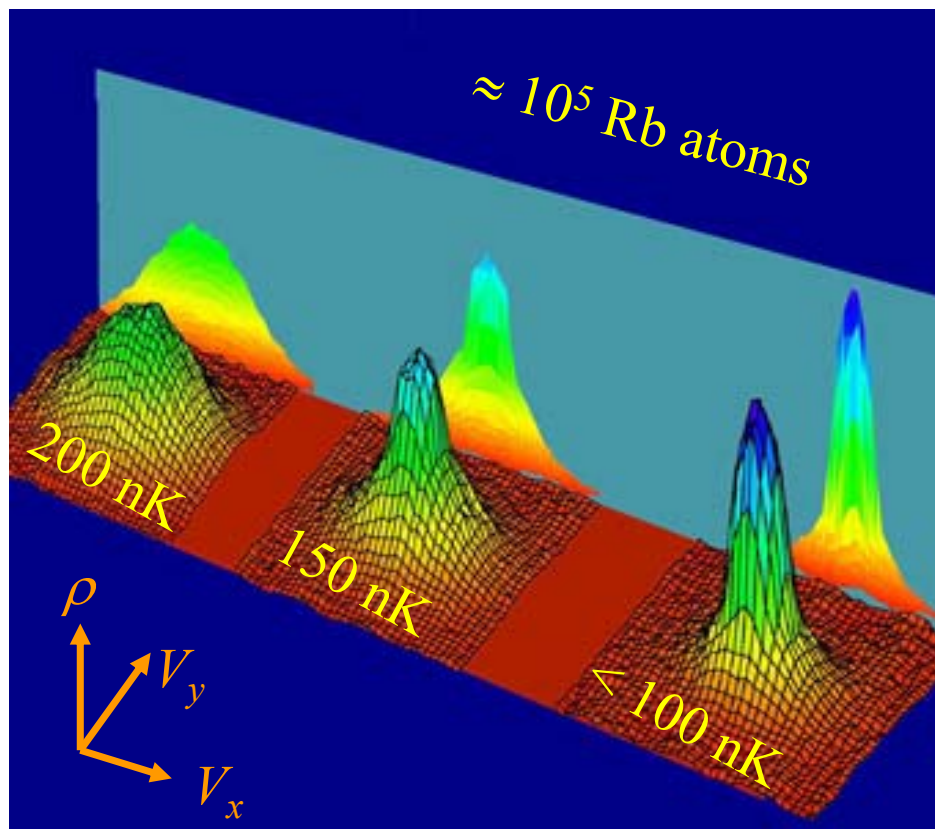
Non ideal trapped quantum gases

1. **Critical temperature shift and other thermodynamics properties in Rb**
2. Penning ionization rate constants and scattering length in He*
3. Roughness of atom chip trapping potential

standard
methods
revisited

- Critical temperature shift (F. Gerbier et al., PRL 92, 030405, 2004)
- Condensed fraction, interaction energy, equilibrium shape of a mixed profile... (F. Gerbier et al., PRA 70, 013607, 2004)

- Turn off the trap at $t = 0$
- Ballistic expansion, duration τ
- Absorption imaging
 - * **Thermal component** (Bose function, Gaussian wings):
mostly thermal velocity
 - * **Condensate** (Thomas Fermi profile, inverted parabola):
mostly interaction energy



- Measurements difficult at a few percent level
- Theoretical issue: expansion of an interacting mixed cloud?

Critical temperature of a trapped Bose gas

Ideal (non-interacting) trapped Bose gas

$$T_c^{\text{ideal}} = T_c^0 - \frac{\zeta(2)}{\zeta(3)} \frac{\hbar(\omega_z + 2\omega_{\perp})}{6k_B}$$

Thermodynamics limit

$$n\Lambda_T^3 = 2.612$$

« Finite size » effects

2% with our parameters

$$\omega_{\perp} / 2\pi = 413 \text{ Hz}$$

$$\omega_z / 2\pi = 8.69 \text{ Hz}$$

Critical temperature of a non ideal Bose gas

Effect of interactions?

Uniform case (box)

- Theory: $T_c \nearrow$ because of density fluctuations (a hot topics)
- Observed with dilute LHe on Vycor

Harmonic trap

- Theory: $T_c \searrow$ for repulsive interaction because of density decrease at the trap center (Einstein criterium unchanged):

W. Krauth; Giorgini et al. (1996)

$$\frac{T_c - T_c^{\text{ideal}}}{T_c^0} \approx -1.33 \frac{a}{a_{\text{HO}}}$$

- Observation?

Critical temperature of a trapped non ideal Bose gas

A “review” of the observations

Inconclusive experiments, except for a pioneering observation (1 standard deviation) by Ensher et al. (1996).

| work | measured $\Delta T_c / T_c^{\text{ideal}}$ |
|-------------|--|
| Mewes 1996 | (assumed 0.0) |
| Ensher 1996 | -0.06 ± 0.05 |
| Han 1998 | -0.04 ± 0.15 |
| Shreck 2001 | 0.0 ± 0.2 |
| Maragò 2001 | 0.00 ± 0.03 |

Improved measurements in Orsay: some experimental tips

Fight shape oscillations occurring at condensation

- Slow down evaporation near condensation (200 kHz / s)
- Hold time (1 s) with RF knife on

Excellent control of the evaporating knife position above trap bottom

- Temperature reproducibility: 20 nK

Accurate absorption measurement of atom number

- Careful calibration of absorption cross section by expansion energy measurement (relies on the value of the scattering length, accurately known from spectroscopy)

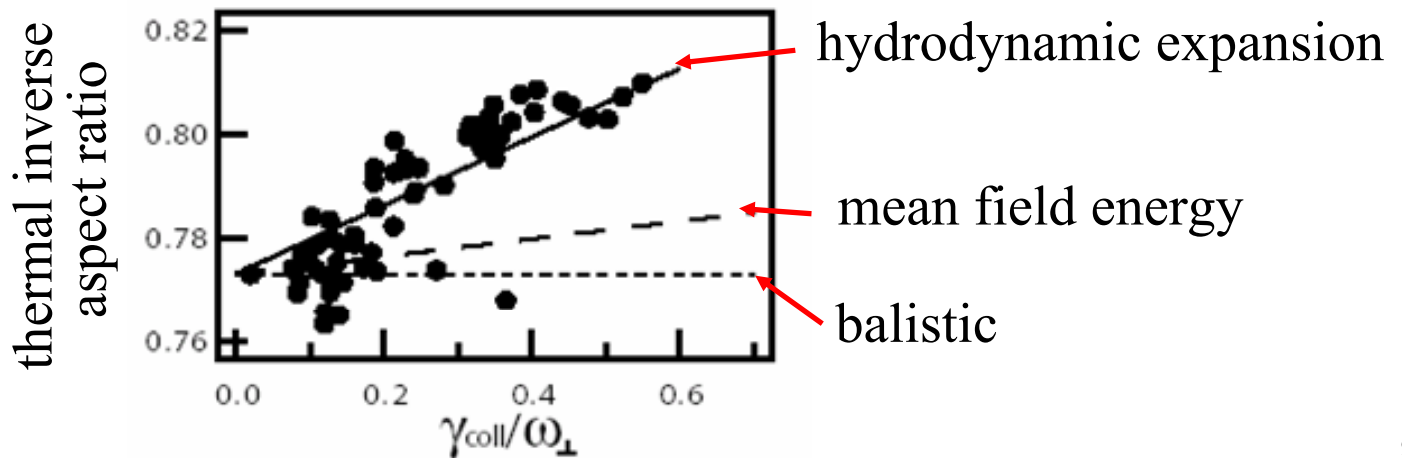
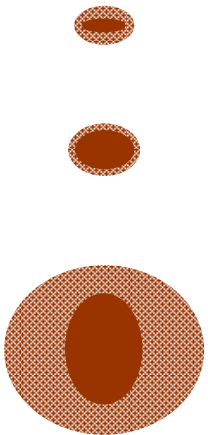
Correction for hydrodynamic effects in temperature measurements

Temperature measurement

Hydrodynamic effects

Temperature measurement: fitting a Bose profile to the wings of the TOF of the cloud around T_c

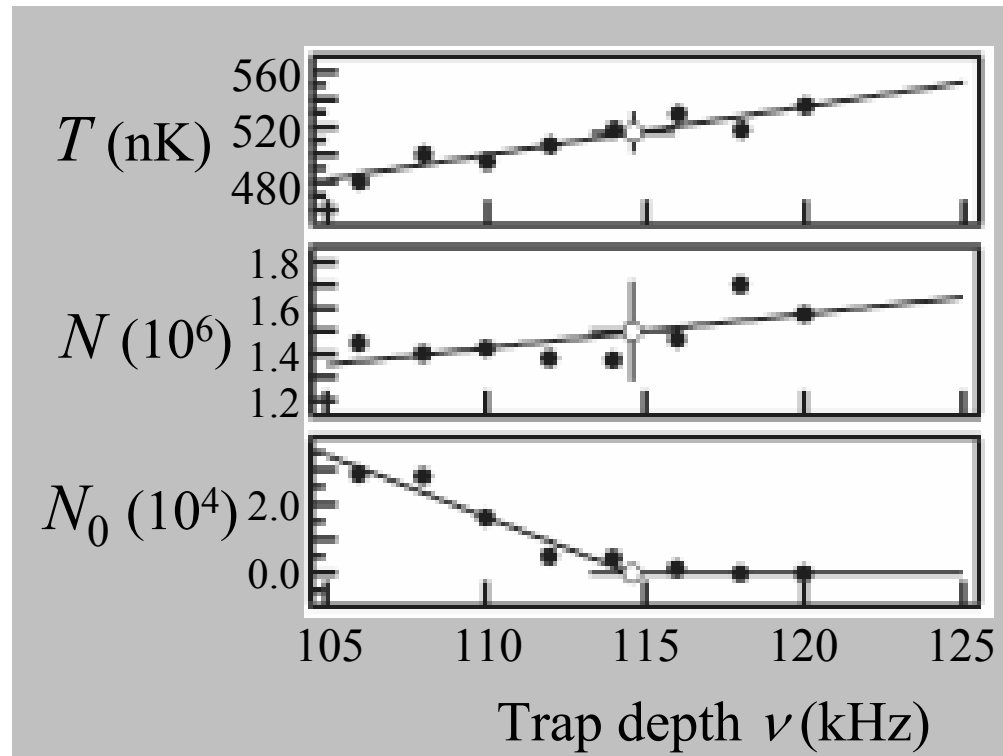
Necessary to **correct hydrodynamic effect** for large and dense thermal clouds (elongated trap $\omega_z / \omega_{\perp} \simeq 45$). Also in Amsterdam.



Acurate determination of the critical point

Very reproducible evap. ramps, stopped at different values of trap depth ν :

- plot T, N, N_0 vs. ν
- linear fits
- find ν_c
- derive N_c and T_c



See estimated error bars

Critical temperature of a trapped ^{87}Rb Bose gas: results

- Non ideal behavior (effect of interactions) observed at the level of 2σ
- Good agreement with mean field theory: fit of ΔT by $\alpha N^{1/6}$ yields:

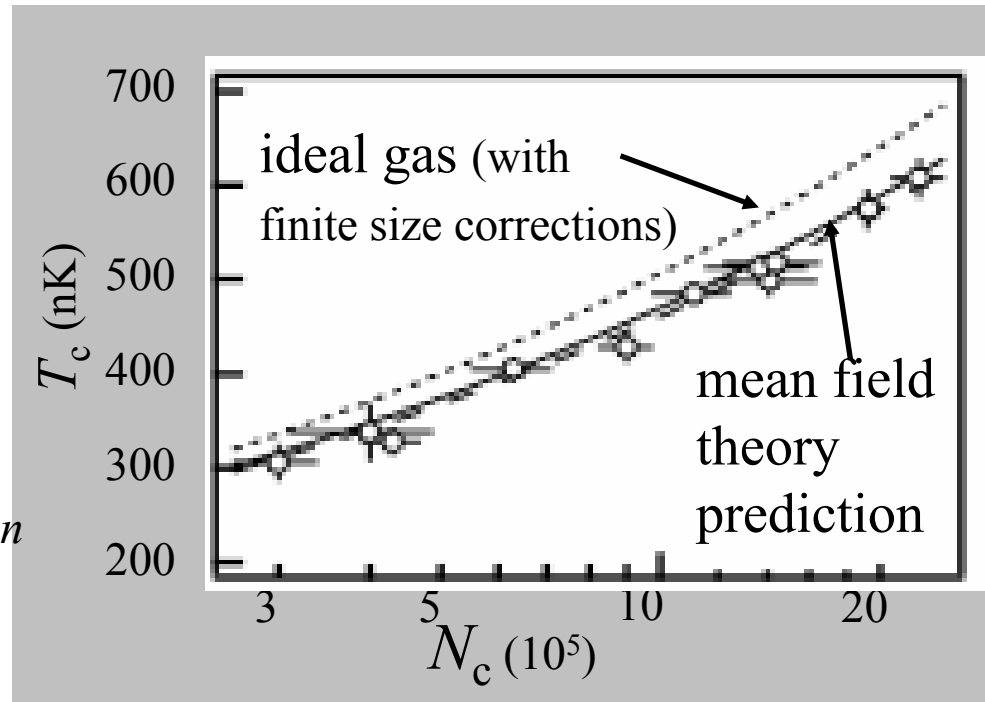
$$\alpha_{\text{exp}} = -0.009(1)_{-0.002}^{+0.003}$$

calibration

statistical

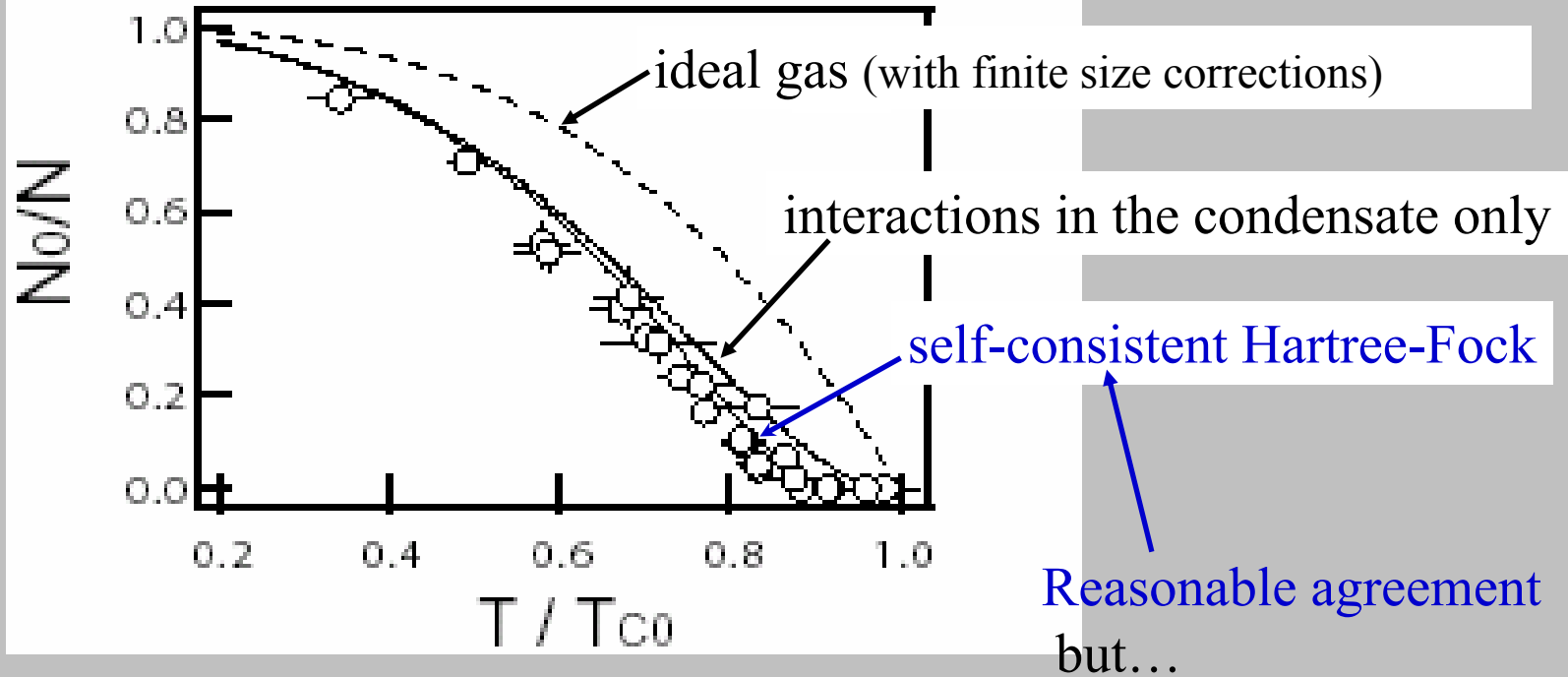
to be compared to

$$\alpha_{\text{th}} = -0.007$$



- No upwards shift due to density fluctuations as predicted for homogeneous case: in agreement with predicted suppression for trapped Bose gases (Giorgini, Pitaevski, Stringari; Arnold and Tomasik)

Trapped ^{87}Rb Bose gas: condensed fraction



...experiment systematically (slightly) below theory

Error in temperature measurement due to interaction between thermal cloud and BEC during expansion? Theory is missing for expansion of a mixed cloud!

Trapped interacting degenerate Bose gas (Rb): conclusions

Deviation from ideal gas clearly observed

Agreement with mean field theory

- Shift of critical temperature
- Self consistent Hartree Fock modeling of condensed fraction and mixed cloud profile

Observation of hydrodynamics effects in TOF of dense thermal cloud

Theory needed to better understand TOF of mixed sample (condensate and thermal cloud)

No effect observed beyond mean field for a **trapped** BEC: **agreement with theory**

Non ideal trapped quantum gases

1. Critical temperature shift and other thermodynamics properties in Rb
2. Penning ionization rate constants and scattering length in He*
3. Roughness of atom chip trapping potential



new
methods

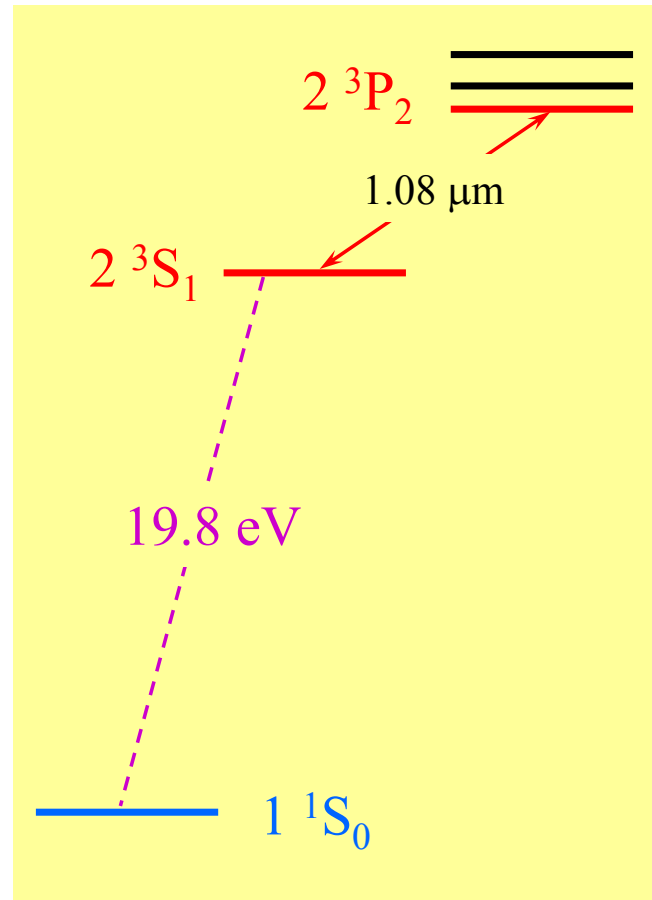
O. Sirjean et al., PRL 89(22): 220406 (2002)

S. Seidelin et al., PRL in print

Metastable Helium $2\ ^3S_1$

- Triplet ($\uparrow\uparrow$) $2\ ^3S_1$ cannot *radiatively* decay to singlet ($\uparrow\downarrow$) $1\ ^1S_0$ (lifetime 9000 s)
- Laser manipulation on closed transition $2\ ^3S_1 \rightarrow 2\ ^3P_2$ at $1.08\ \mu\text{m}$ (lifetime 100 ns)

- Large electronic energy stored in He*
 - \Rightarrow ionization of colliding atoms or molecules
 - \Rightarrow extraction of electron from metal: single atom detection with Micro Channel Plate detector



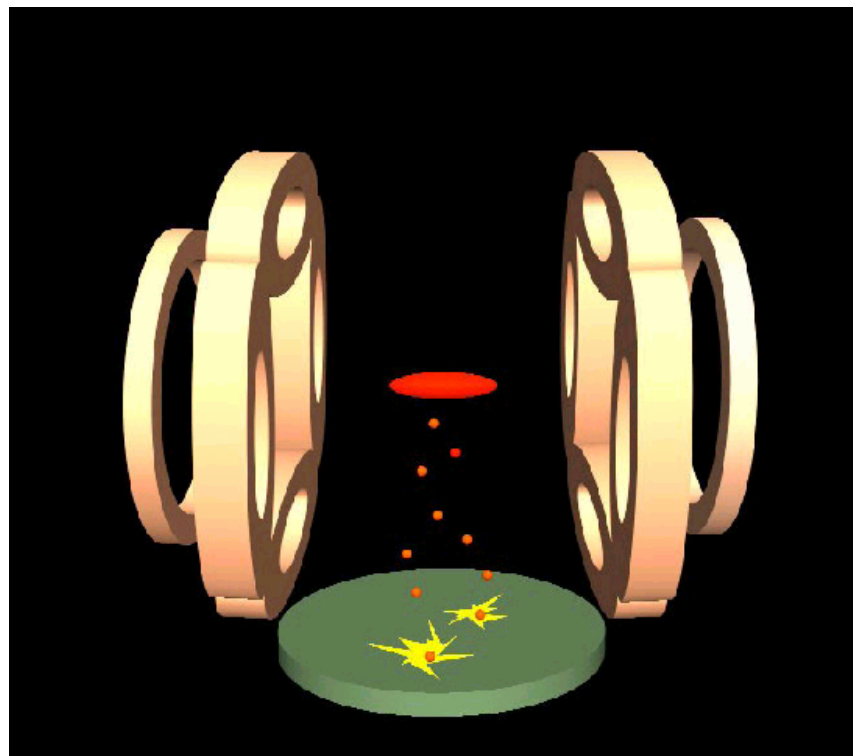
Clover leaf trap

@ 240 A : B_0 : 0.3 to 200 G ;

B' = 90 G / cm ; B'' = 200 G / cm²

$\omega_z / 2\pi = 50$ Hz ; $\omega_{\perp} / 2\pi = 1800$ Hz

(1200 Hz)



He* on the Micro Channel Plate detector:

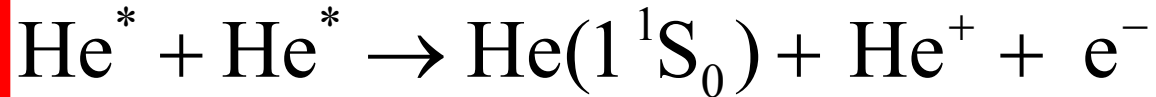
⇒ an electron is extracted

⇒ multiplication

⇒ observable pulse

Single atom detection of He*

Penning ionization of He*



Reaction constant $\approx 5 \times 10^{-10} \text{ cm}^3 \cdot \text{s}^{-1}$ @ 1 mK

\Rightarrow low density \Rightarrow no fast thermalization \Rightarrow no evaporative cooling ☹️

Solution (theory, Shlyapnikov et al., 1994; Leo et al.):

Penning ionization strongly suppressed (10^{-5} predicted!) in spin polarized He* because of selection rule (spin conservation)

$$m = 1 + m = 1 \quad \not\rightarrow \quad s = 0 + s = 1/2 + s = 1/2$$

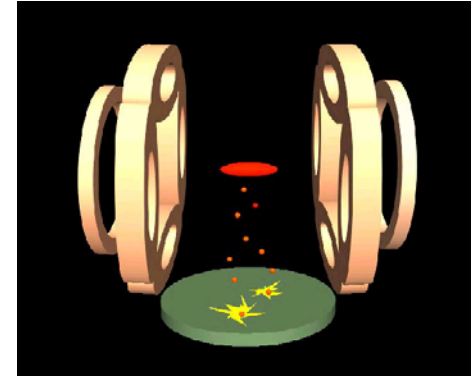
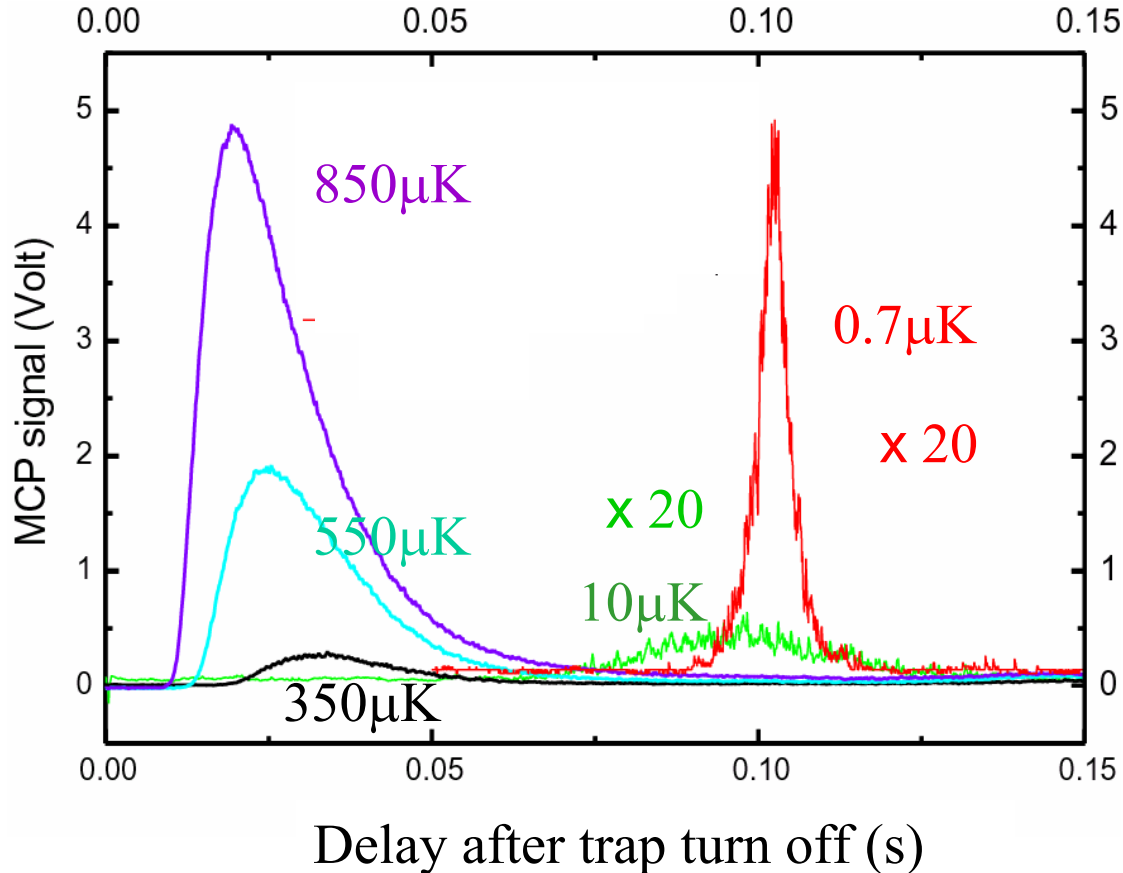
Magnetically trapped He* *is* spin polarized ☺️

Preliminary experimental evidence (Amsterdam, Orsay, 1999): suppr. $< 10^{-2}$

Definitive evidence of suppression ($< 10^{-4}$): **BEC of He* observed** (Orsay, Paris, 2001)

Evaporative Cooling to BEC

Time of flight on the MCP

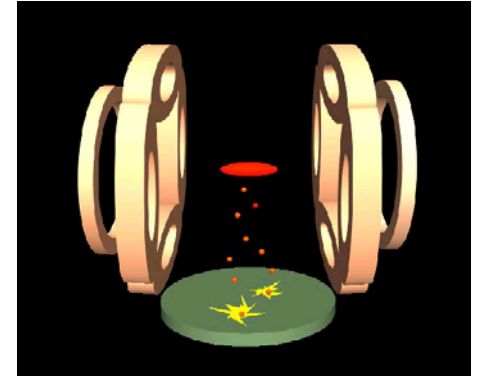


- RF ramped down from 130 MHz to ~ 1 MHz in 70 s (exponential 17 s)
 \Rightarrow less atoms, colder
- Small enough temp. (about $2\mu\text{K}$): all atoms fall on the detector, better detectivity
- At $0.7\mu\text{K}$: narrow peak, BEC

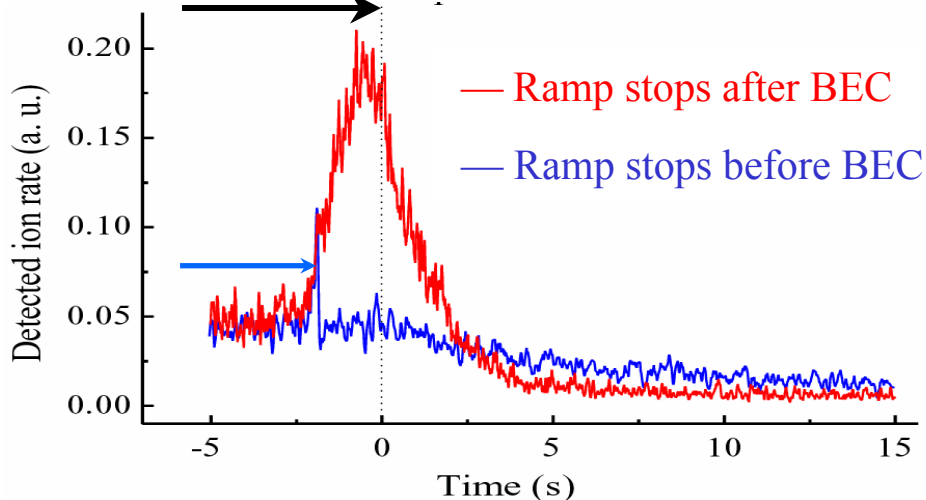
Residual Penning ionization

A new tool for monitoring a trapped He* BEC

- Residual ionization (He⁺): detected with negatively biased grid (2keV) in front of MCP in counting mode (from 10² to 10³ s⁻¹)



evaporative cooling



Real time observation of BEC birth and death on a single sample

Interpretation: ionization increases with density (2 and 3 body Penning ionization)

Quantitative if one knows the Penning ionisation rate constants

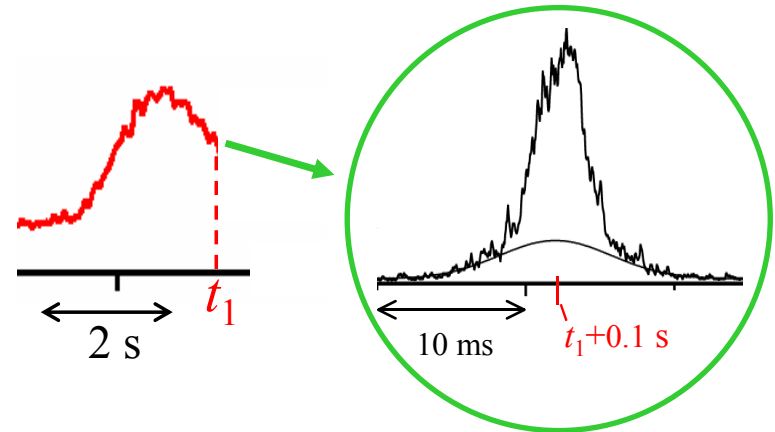
Ionization monitoring plus TOF: a measurement of Penning ionization constants

Complete ion rate measurement $I(t_1)$ by measurement of the spatial distribution of atoms at t_1

⇒ Switch off the trap at t_1 and observe
Time of Flight of the released atoms:

⇒ Atom number in the condensate

⇒ Atom number and temperature in the thermal cloud

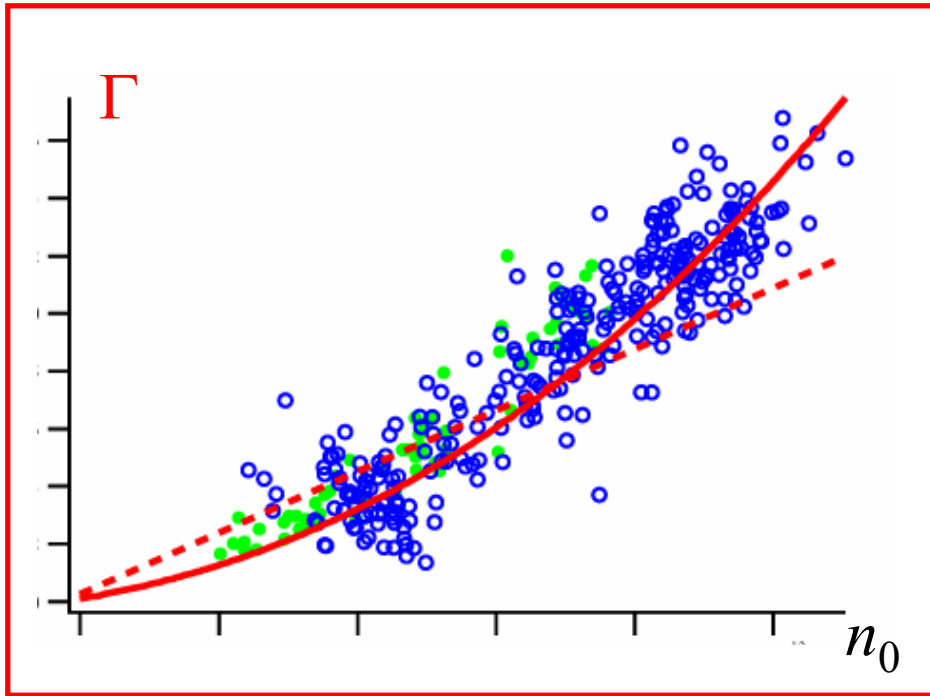


One can then know, in a given situation (at t_1) :

- the ion rate per atom $\Gamma(t_1)$
- the atomic density $n(\mathbf{r}, t_1)$

⇒ ionization rate constants β (2 body) and L (3 body)

Ion rate per atom vs peak density in a quasi pure BEC



For each ion rate I , TOF:

$\Rightarrow N_0$ (atom number)

$\Rightarrow n_0$ (density)

\Rightarrow check pure BEC (thermal cloud not visible, i. e. $< 10\%$)

\Rightarrow ion rate per atom $\Gamma = \frac{W}{N_0}$

Fit to $\Gamma = \frac{2}{7} \kappa_2 \beta n_0 + \frac{8}{63} \kappa_3 L n_0^2 \Rightarrow \beta, L$: 2 and 3 body ionization

The detection efficiency and scattering length issue

A serious difficulty: determining the absolute atom number

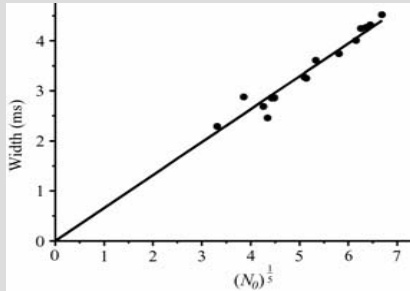
- Absolute **detection efficiency** of MCP known within a factor of 2

Another difficulty: determining the absolute atomic density in the BEC

- Depend on **scattering length** a

Scattering length

obtained from measurement of expansion velocity of a pure condensate



$$W_i \propto (N_0 a)^{1/5}$$

Accuracy on a depends on accuracy on atom number N_0 i.e. on **detection efficiency**

First value of a (detection efficiency estimated)

$$a = 20 \pm 10 \text{ nm}$$

Uncertainties on a and detection eff. « entangled »: only one unknown factor

Detection efficiency and scattering length issue: a solution

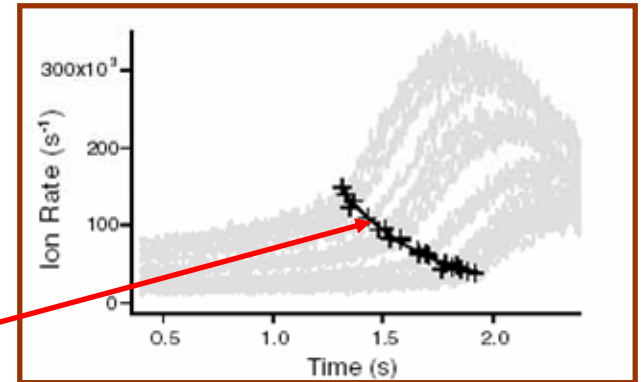
Our results on Penning ionization constants depend dramatically on the value of a . Photoassociation spectroscopy measurements of a ?

Another solution: improve the accuracy on atom detection efficiency

Calibration based on **absolute atom number** derived from **thermodynamics relation at BEC transition**

accurately measured by TOF $N_c = f(T_c)$

accurately located by sudden rise of ion current



$$a = 11.3_{-1.5}^{+2.5} \text{ nm}$$

Reasonable agreement with theory and previous measurements.

Reduced error bars

Combining with independent measurements of a ?

Combining our results to a photoassociation spectroscopy measurement of a (in progress at ENS):

⇒ More accurate value expected

⇒ Independent measurement: will allow us to reinterpret our results and test various effects depending on a :

- critical temperature correction
- quantum depletion (30% correction in 3-body Penning ionization)

Combining different methods: great tool

Penning ionization: an original tool for « non destructive » monitoring of a trapped He* gas

Non ideal trapped quantum gases

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3. **Roughness of atom chip trapping potential**

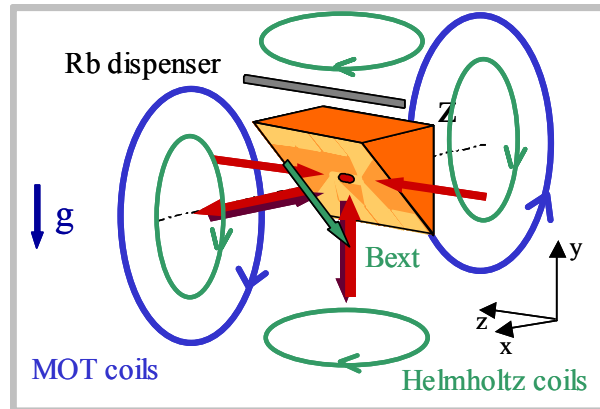
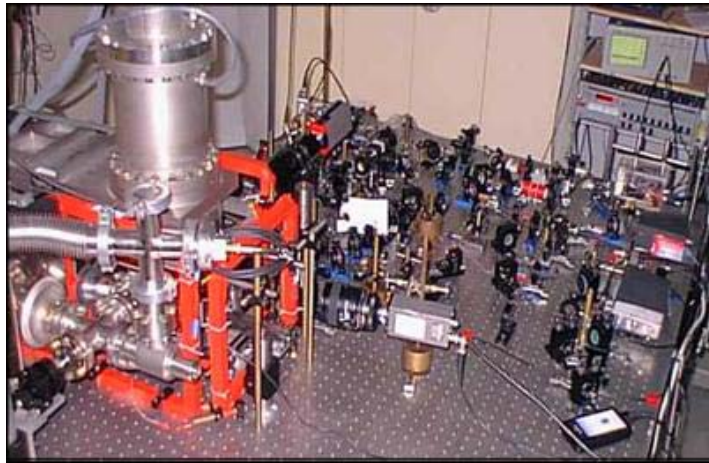
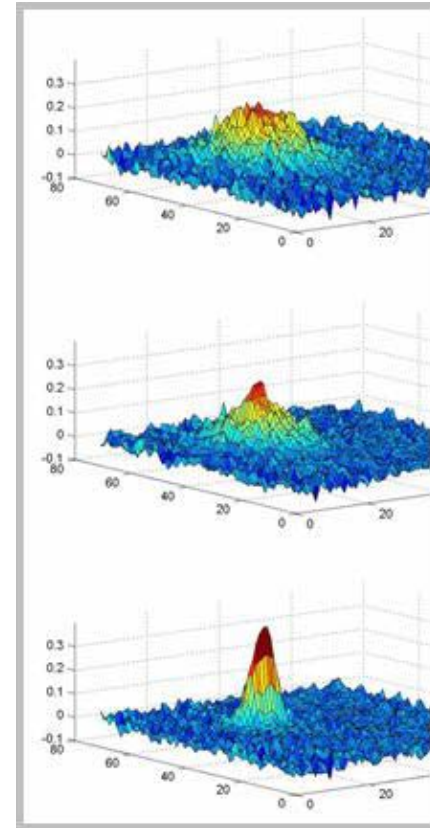
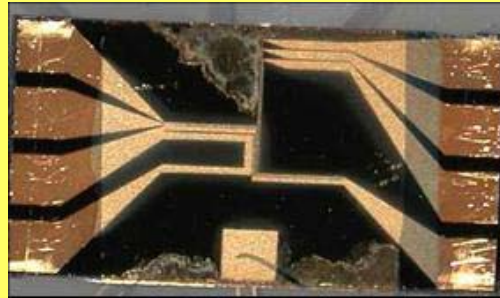
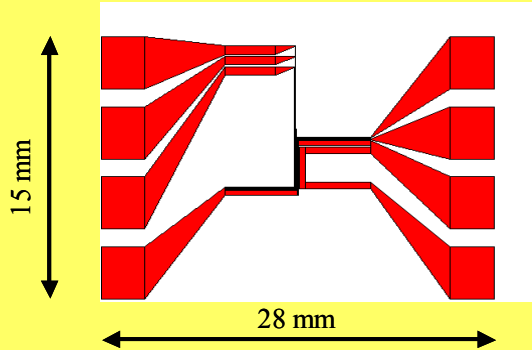
non ideal
trapping
potential

J. Estève, C. Aussibal, **T. Schumm**, C. Figl, D. Mailly, I. Bouchoule, C. I. Westbrook, and A. A., *Phys. Rev. A*, in press

T. Schumm, J. Estève, C. Figl, J.-B. Trebbia, C. Aussibal, H. Nguyen, D. Mailly, I. Bouchoule, C. I. Westbrook and A. A., [Physics/0407094](#)

BEC on a chip in Orsay

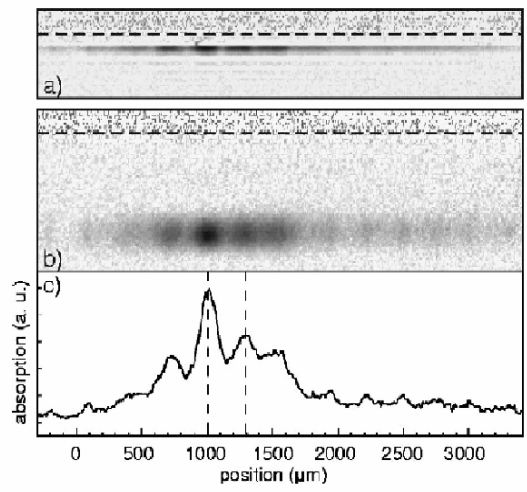
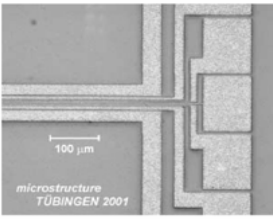
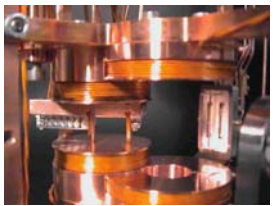
Magnetic trap with microfabricated gold wires on silicon (LPN, Marcoussis)



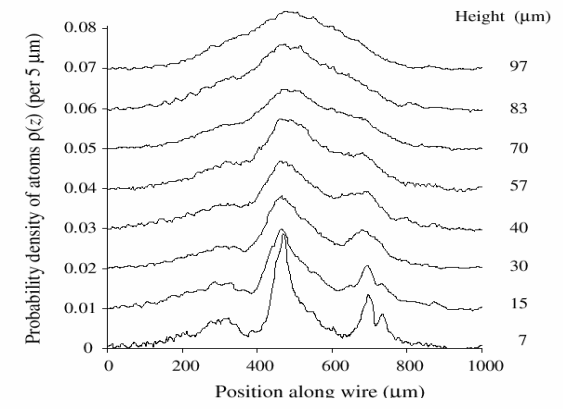
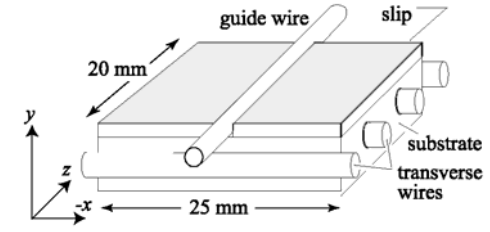
« Small » experiment

BEC on a chip: fragmentation

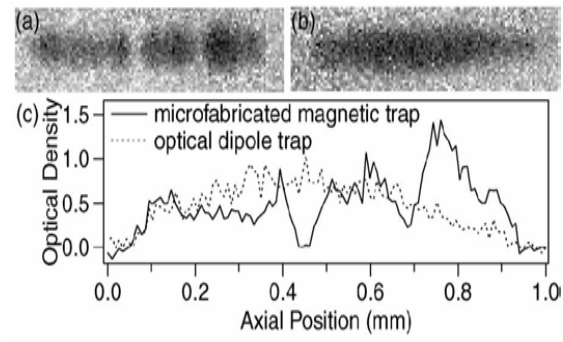
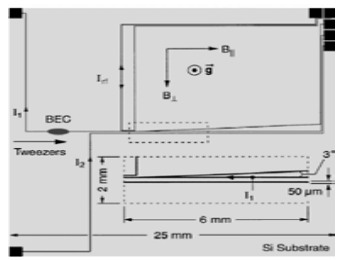
Tübingen



Sussex / London



MIT



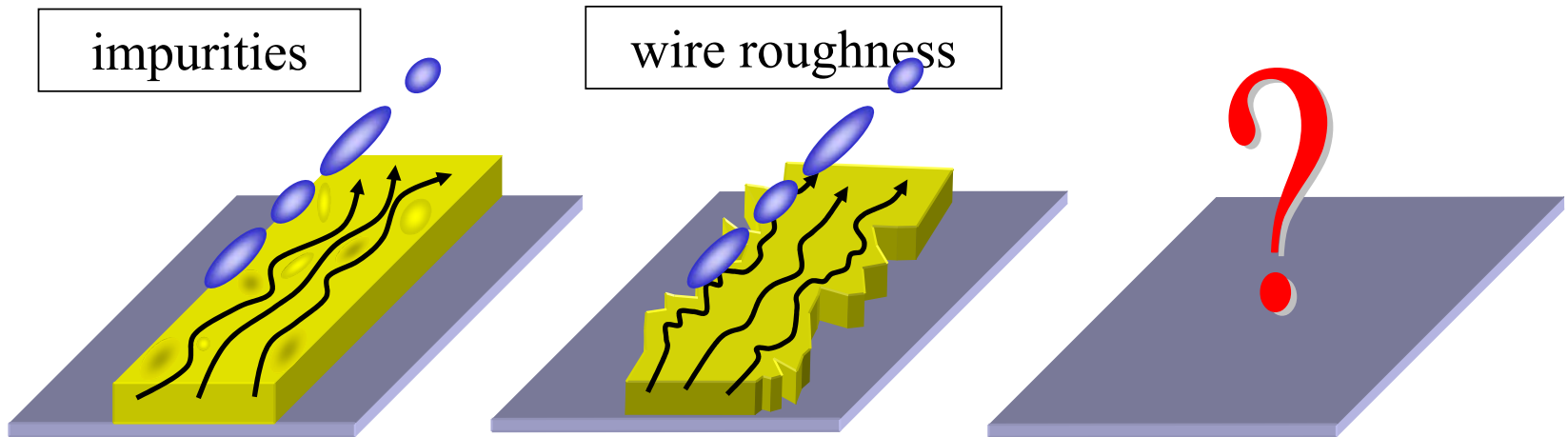
Orsay

also!

In search of the cause of fragmentation

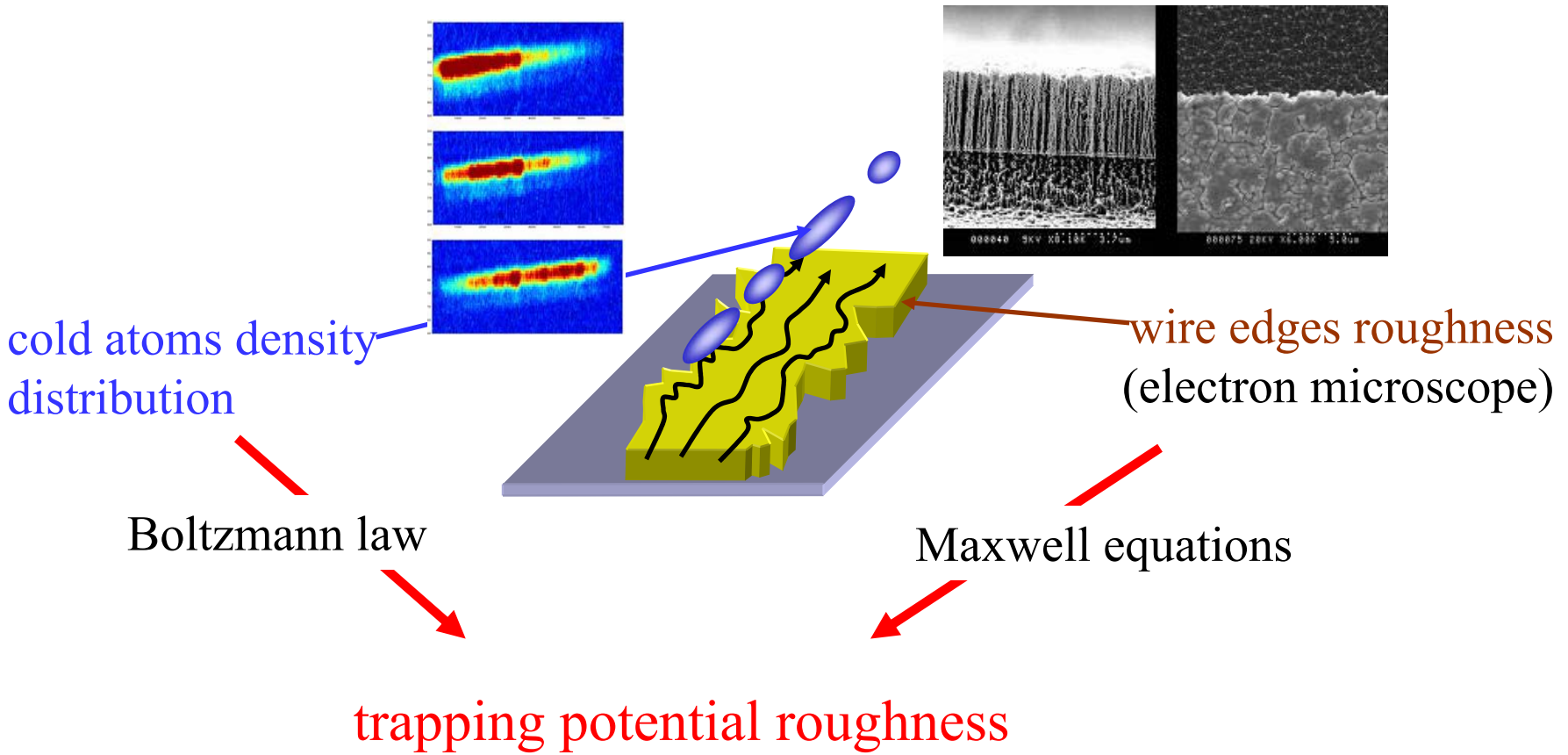
Fragmentation due to roughness of the magnetic trapping potential, due to deviations of the current flow (static, linear in current, decreasing with distance to the wire...)

Cause of deviations in current flow?



proposed D. Wang, M. Lukin, and
E. Demler, cond-mat/0307402

Our approach: measure trapping potential roughness and wire edges roughness

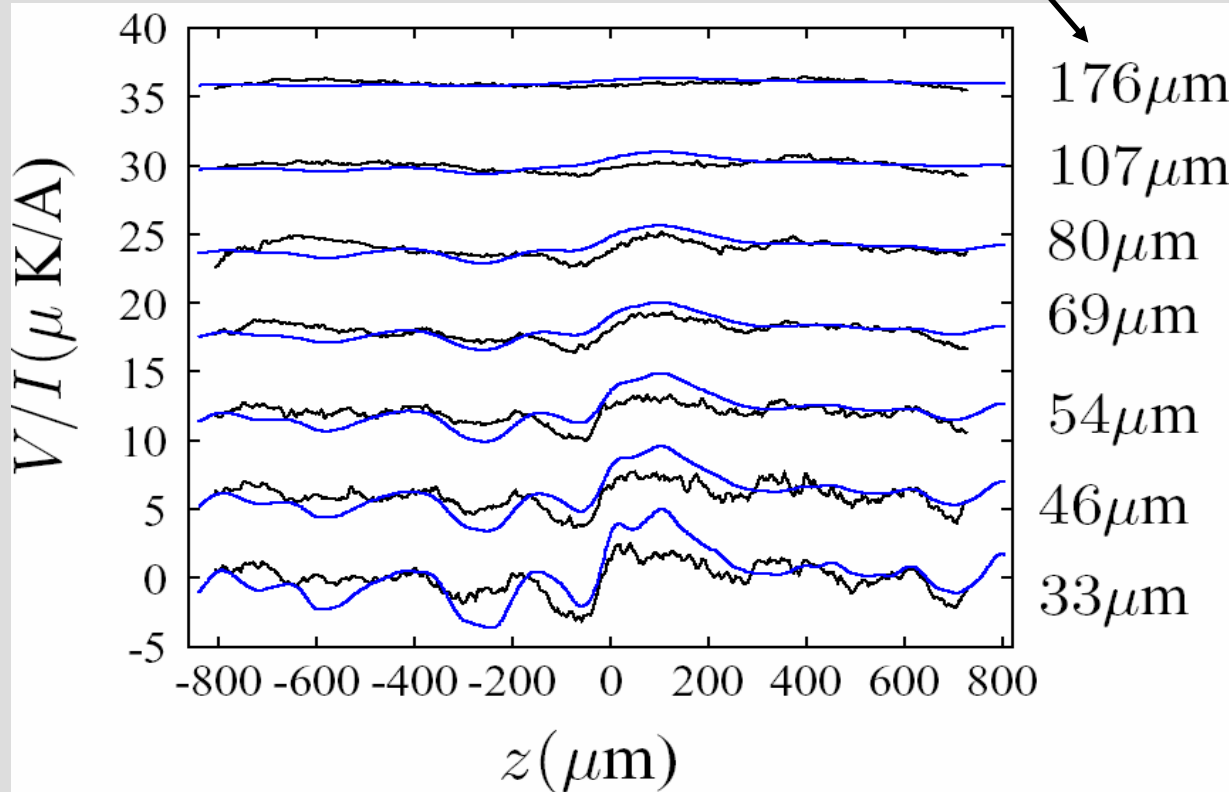


• Our conclusion: in our chip wire edges roughness suffices to explain trapping potential.



roughness

distance from chip



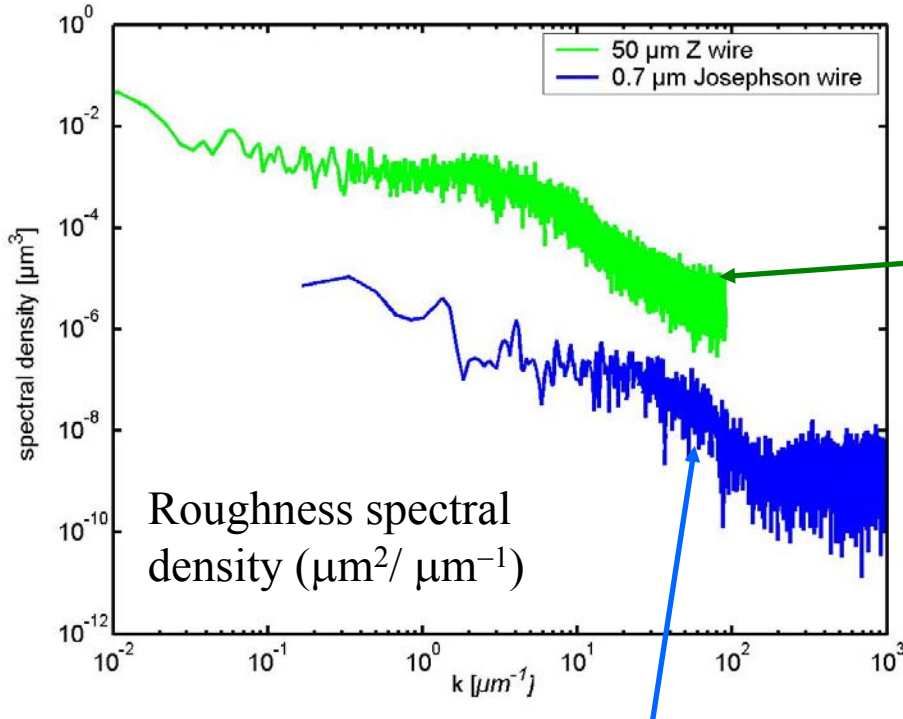
— reconstructed from density profiles of cold atoms

— reconstructed from edges roughness measurements

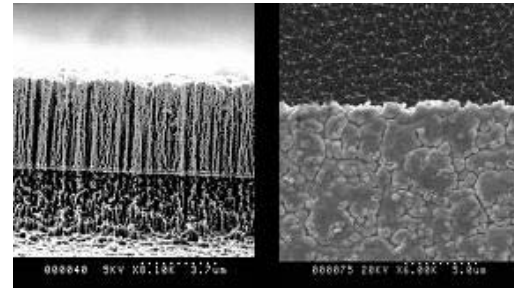
no free parameters!

Comparison of roughness power spectrum also convincing

Conclusion: go for new technology

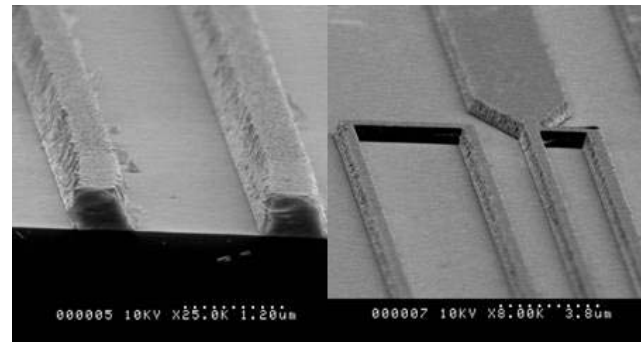


Orsay 1st generation:
electroplated gold wires
(5 μm x 50 μm) on
silicon wafer:



Orsay 2nd generation: 700 nm width
evaporated gold wires, pattern
written with e beam

In progress...



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He* BEC
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BEC VERSATILE SOURCE
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Jean Felix Riou
William Guérin

K-Rb MIXTURES
Gaël Varoquaux
Rob Nyman
Yann Le Coq

BIOPHOTONICS
Karen Perronet

PHD and post doc applications encouraged

That's all