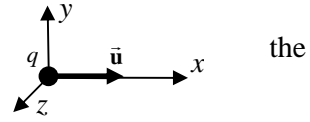


## PHYS2100 Tutorial 2

**Problem 2.1** Follow the way in which the transformation for  $B_2$ ,  $B_3$ , and  $E_1$  have been derived (see Lecture notes) and obtain transformations for  $B_1$ ,  $E_2$ ,  $E_3$

**Problem 2.2** Calculate the field created by an electrical charge moving with a constant velocity  $u$  (as shown in figure).



**Problem 2.3.1.** Prove that for any particle  $\mathbf{P}^2 = m^2 c^2$ . This relation also holds for photons.

**Problem 2.3.2.** Elastic collisions preserve the rest masses of all involved particles.

Prove that for elastic collisions  $\mathbf{P}_b^2 = \mathbf{P}_a^2$ , where  $a$  and  $b$  refer to “before collision” and “after collision”, holds for any involved particle.

**Problem 2.3.3.** Prove that if two particles collide elastically then  $\mathbf{P}_{b1} \cdot \mathbf{P}_{b2} = \mathbf{P}_{a1} \cdot \mathbf{P}_{a2}$ .

**Problem 2.3.4.** Prove that the relative velocity of two elastically colliding particles does not change after collision.

**Problem 2.4.** A particle of mass  $M_b$  splits at rest in two parts one of which is a light article of mass  $m \ll M_b$  and the second part is a heavy particle of mass  $M_a$ . The light particle moves with a relativistic velocity  $v$ . The massive part moves with velocity  $u \ll c$  and  $u \ll v$ . All velocities are in the reference frame where the original particle was at rest.

Prove that the classical momentum conservation law in the form  $\Delta M v + M_a u = 0$ ,

$\Delta M = M_b - M_a$  holds for any value of  $v$  (even for  $v \approx c$ ).